Teacher Energized Resource Manual

Class : 8th Subject : Mathematics



CENTRAL BOARD OF SECONDARY EDUCATION

Preface

In consonance with the move towards outcome-based education where focus is on developing competencies in students, the Central Board of Secondary Education is delighted to share the *Teacher Energized Resource Manual* that will aid teachers in aligning their classroom transaction to a competency framework.

Each chapter of the Resource Manual corresponds to the respective chapters in the NCERT textbooks. The chapters have been chunked by concept; these concepts have been linked to the NCERT Learning Outcomes; and an attempt has been made to delineate Learning Objectives for each concept. Every chapter has a set of assessment items, where two items have been provided as examples for each Learning Objective. Teachers can use these to assess if the learner has acquired the related concept. Needless to say, the items are illustrative examples to demonstrate how competency-based items can be prepared to measure Learning Objectives and Outcomes. The variety in item forms is suggestive of the ways in which a particular concept can be assessed to identify if the learner has attained different competencies. We trust and hope that teachers would be able to generate many more similar test items for use in practice.

Your observations, insights and comments as you use this Resource Manual are welcome. Please encourage your students to voice their suggestions as well. These inputs would be helpful to improve this Manual as these are incorporated in the subsequent editions. All possible efforts have been made to remove technical errors and present the Manual in a form that the teachers would find it easy and comfortable to use.

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HOW TO USE THIS MANUAL

The goal of the Teacher Energized Resource Manual (TERM) is to provide teachers with competency-based education resources aligned to NCERT textbooks that would support them in the attainment of desired Learning Outcomes and development of requisite competencies of the learner. The TERM has equal number of corresponding chapters as NCERT Textbooks with listing of Concepts, Learning Outcomes developed by NCERT and Learning Objectives. Competency based test items for each corresponding Learning Objective and sample activities for enrichment have been provided.

Learning Objectives:

Each chapter has a *Learning Objectives* table. The table also lists the Concepts covered in the chapter. Learning Objectives are broken down competencies that a learner would have acquired by the end of the chapter. They are a combination of skills and what the learner would use this skill for. For example, the first Learning Objective in the table below relates to the skill of *application* and the students will use this competency to obtain the highest common factor of 2 positive integers. Teachers can use these specific Learning Objectives to identify if a student has acquired the associated skill and understands how that skill can be used.

| Concepts | Learning Objectives | Learning Outcomes |
|---|--|--|
| Evolid's Division | Apply Euclid Division Algorithm in order to obtain HCF of 2 positive integers in the context of the given problem | |
| Euclid & Division | Apply Euclid Division Algorithm in order to prove results of positive integers in the form of ax+b where a and b are integers | Commission of sumbars and |
| Fundamental | Use the Fundamental Theorem of Arithmetic in | Generalises properties of numbers and |
| Theorem of Arithmetic | order to calculate HCF and LCM of the given numbers in the context of the given problem | to evolve results, such as, Euclid's |
| Irrational Numbers | Recall the properties of irrational number in order to prove that whether the sum/difference/product/quotient of 2 numbers is irrational or not | theorem of arithmetic in order to apply them to solve problems related to real life contexts |
| | Apply theorems of irrational number in order to prove whether a given number is irrational or not | |
| Decimal | Apply theorems of rational numbers in order to | |
| Representation of Irrational Numbers | find out about the nature of their decimal representation and their factors | |

Concepts:

The important concepts in a particular chapter are listed in the first section. Most often, they follow a logical order and present a sequence in which these are likely to be covered while teaching. In case, your teaching strategy is different and presents them in a different order, you need not worry. Teach the way, you consider the best. You only need to ensure their understanding and the attainment of desired learning objectives.

Learning Outcomes (NCERT):

A mapping of Learning Outcomes developed by the NCERT and Learning Objectives is provided in last column of the table. The Learning Outcomes have been developed by the NCERT. Each Learning Objective is mapped to NCERT Learning Outcomes and helps teachers to easily identify the larger outcome that a learner must be able to demonstrate at the end of the class/ chapter.

Test items:

For each Learning Objective, at least two competency-based test items have been provided. Although, the items in this resource manual are multiple choice questions, which assess developed competencies of a student rather than only knowledge, it must be kept in mind that there can be different kinds of assessment that can easily align with competency-based education. Teachers can use these items to assess if a learner has achieved a particular Learning Objective and can take necessary supportive actions. Teachers are also encouraged to form similar questions which assess skills of students.

| LOB: Apply Euclid Division Algorithm in order to obtain HCF of 2 given numbers in the context of the given | | | |
|---|--|--|--|
| problem | | | |
| A worker needs to pack 350 kg of rice and 150 kg of wheat in bags such that each bag weighs the same. | | | |
| Each bag should either contain rice or wheat. Which option shows the correct steps to find the greatest | | | |
| amount of rice/wheat the worker can pack in each bag? | | | |
| Option I: Step 1: $350 = 2(150) + 50$ | | | |
| Step 2: $150 = 3(50) + 0$ | | | |
| Step 3: Greatest amount: 50 kg | | | |
| Option 2: Step 1: $350 = 2(150) + 50$ | | | |
| Step 2: $150 = 2(50) + 0$ | | | |
| Step 3: Greatest amount: 50 kg | | | |
| Option 3: Step 1: $350 = 2(150) + 50$ | | | |
| Step 2: $150 = 3(50) + 0$ | | | |
| Step 3: Greatest amount: 150 kg | | | |
| Option 4: Step 1: $350 = 2(150) + 50$ | | | |
| Step 2: $150 = 2(50) + 0$ | | | |
| Step 3: Greatest amount: 150 kg | | | |
| Correct Answer: Option | | | |
| | | | |

Fig: 3

Suggested Teacher Resources

At the end of each chapter, certain activities have been suggested which can be carried out by the teachers with learners to explain a concept. These are only samples and teachers can use, adapt, as well as, create activities that align to a given concept.

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RATIONAL NUMBERS

QR Code:

Ι.



Learning outcome and Learning Objectives:

| Content area / Content area / Conceptss | Learning Objectives | Learning Outcome |
|---|---|--|
| Introduction to Rational Numbers | Define rational number in order to identify whether the given number is a rational number or not Apply the properties of natural numbers, whole numbers and integers with respect to all the arithmetic operations in order to extend them for rational numbers Use prior knowledge in order to define the additive and multiplicative identity of rational numbers. Use prior knowledge of integers and fractions in order to define the additive and multiplicative inverse of rational numbers. Apply Distributivity of multiplication over addition for rational numbers in order to simplify a given expression | Explores patterns in arithmetic operations in order to generalise properties of addition, subtraction, multiplication and division for rational numbers |
| Representation of Rational Numbers on the Number Line | Extend the concepts of number line in order to represent rational number on the number line | |
| Rational Numbers between Two Rational Numbers | Calculate and find rational numbers between any two rational numbers in order to prove that there are infinite rational numbers between any two given rational numbers | Calculate rational numbers between any two given rational numbers in order to prove that there are infinite rational numbers between two rational numbers |

Test items



LOB: Define rational number in order to identify whether the given number is a rational number or not.

I. Is -0.4 a rational number?

Option I: No, because it cannot be written in the form of $\frac{p}{q}$.

Option 2: Yes, because it can be written in the form of $\frac{p}{a}$.

Option 3: Yes, because it is a negative number.

Option 4: No, because it is a decimal number.

Correct Answer: Option 2

2. Consider the expression below:

 $\sqrt{\frac{1}{k+7}}$

Given that the expression represents a rational number, which of these is the least possible positive integer value of k?

Option 1: 0 Option 2: 2 Option 3: 8 Option 4: 10 Correct Answer: Option 2

LOB: Apply the properties of natural numbers, whole numbers and integers with respect to all the arithmetic operations in order to extend them for rational numbers.

I. Which of these options completes the sentence below?

The equation $\frac{-25}{9} - \frac{7}{3} = \frac{-46}{9}$ shows that _____. **Option 1:** rational numbers are not closed under subtraction **Option 2:** rational numbers are not closed under division **Option 3:** rational numbers are closed under subtraction **Option 4:** rational numbers are closed under division **Correct Answer:** Option 3

2. Consider the equation below. $\frac{5}{6} + \left(\frac{1}{8} + \frac{16}{5}\right) = A + \frac{1}{8}$ Which of these is equivalent to A? **Option 1:** $\frac{5}{48} + \frac{16}{5}$ **Option 2:** $\frac{5}{6} + \frac{1}{8}$ **Option 3:** $\frac{1}{8} + \frac{16}{5}$ **Option 4:** $\frac{5}{6} + \frac{16}{5}$

LOB: Use prior knowledge in order to define the additive and multiplicative identity of rational numbers.

1. If the multiplicative identity of rational number $\frac{p}{a}$ is x, what could be the value of x?

```
Option I: \frac{q}{p}
Option 2: \frac{p}{q}
Option 3: 0
Option 4: 1
Correct Answer: Option 4
```

2. Which of these statements is true about the rational number $\frac{a}{b}$?

Option 1: The additive identity of rational number $\frac{a}{b}$ is $\frac{a}{b}$. **Option 2:** The additive identity of rational number $\frac{a}{b}$ is $-\frac{a}{b}$

Option 3: The additive identity of rational number $\frac{a}{b}$ is 0. **Option 4:** The additive identity of rational number $\frac{a}{b}$ is 1.

Correct Answer: Option 3

LOB: Use prior knowledge of integers and fractions in order to define the additive and multiplicative inverse of rational numbers.

- 1. Consider the equation $\frac{m}{5} + \left(\frac{-m}{5}\right) = 0$. Which of these is true? **Option 1:** $\frac{-m}{5}$ is the additive inverse of $\frac{m}{5}$. **Option 2:** $\frac{-m}{5}$ is the additive identity. **Option 3:** $\frac{-m}{5}$ is the multiplicative inverse of $\frac{m}{5}$. **Option 4:** $\frac{-m}{5}$ is the multiplicative identity. **Correct Answer:** Option 1
- 2. Consider the equation $\frac{2}{3} \times (p-q) = 1$. Which of these can be the values of p and q? **Option I:** $p = \frac{3}{2}$ and q = 1 **Option 2:** $p = \frac{5}{2}$ and q = 1 **Option 3:** $p = \frac{3}{2}$ and $q = \frac{5}{2}$ **Option 4:** $p = \frac{5}{2}$ and $q = \frac{3}{2}$ **Correct Answer:** Option 2

LOB: Apply Distributivity of multiplication over addition for rational numbers in order to simplify a given expression

- 1. Which of these is equivalent for $\frac{16}{9} \times \left(\frac{5}{7} + \frac{13}{4}\right)$? **Option 1:** $\frac{16}{9} \times \frac{5}{7} \times \frac{13}{4}$ **Option 2:** $\left(\frac{16}{9} \times \frac{5}{7}\right) + \frac{13}{4}$ **Option 3:** $\left(\frac{16}{9} \times \frac{5}{7}\right) + \left(\frac{16}{9} \times \frac{13}{4}\right)$ **Option 4:** $\left(\frac{16}{9} \times \frac{5}{7}\right) \times \left(\frac{16}{9} \times \frac{13}{4}\right)$ **Correct Answer:** Option 3
- 2. Consider the expression below.

$$\frac{-9}{4} \times (\frac{2}{7} + p)$$

If the expression is equal to $\frac{72}{35}$, what is the value of p?

Option I: $\frac{6}{5}$ **Option 2:** $\frac{2}{35}$ **Option 3:** $-\frac{6}{5}$ **Option 4:** $-\frac{2}{35}$

Correct Answer: Option 3

LOB: Extend the concepts of number line in order to represent rational number on the number line

1. Question Text: Which of these letters on the given number line represents $\frac{5}{2}$?



2. If x and y are two natural numbers such that x > 19 and y < 5, which number line represents the location of a point $P = \frac{x}{2+5y}$ such that P has the least possible value?



Correct Answer: Option 3

LOB: Calculate and find rational numbers between any two rational numbers in order to prove that there are infinite rational numbers between any two given rational numbers.

- 1. Which of the following rational numbers lies between $\frac{1}{10}$ and $\frac{9}{4}$?
 - Option 1: $\frac{21}{20}$, $\frac{1}{4}$ and $\frac{3}{80}$ Option 2: $\frac{1}{2}$, $\frac{15}{19}$ and $\frac{11}{15}$ Option 3: $\frac{17}{6}$, $\frac{19}{20}$ and $\frac{53}{4}$ Option 4: $\frac{49}{25}$, $\frac{17}{4}$ and $\frac{2}{3}$ Correct Answer: Option 2
- 2. If x and y are two non-zero positive rational numbers, which of these statements is always true? **Option I:** $\frac{x-y}{2}$ is a rational number between x and y.

Option 2: $\frac{2}{x \times y}$ is a rational number between x and y. **Option 3:** $\frac{x+y}{2}$ is a rational number between x and y. **Option 4:** $\frac{x+y}{2}$ is a rational number between x and y.

Correct Answer: Option 3

Suggested Teacher Resources



Lesson Plan



资料

| Objective | The students will be able to verify the closure and the commutative properties of rational numbers | | |
|---------------------|--|--|--|
| Prerequisite | Properties of integers, rational numbers, arithmetic operations on rational numbers. | | |
| Vocabulary words | Rational number, closure, commutativity. | | |
| Materials required | Chalks, blackboard, duster, notebooks, pencil, chits, chart papers. | | |
| Procedure | The students will be able to verify the closure and the commutative properties of rational numbers Properties of integers, rational numbers, arithmetic operations on rational numbers. Rational number, closure, commutativity. Chalks, blackboard, duster, notebooks, pencil, chits, chart papers. Preparation required before the class: Preparation required before the class: Prepare around 12-20 chits mentioning a rational number on each of them. A sample has been given at the end of the chapter. Equally distribute the chits into two bowls. Arrange a dice wherein faces should show an arithmetic operator (+, -, x, +), one face should mention-'try again' and, the 6th face should mention-'skip'. The teacher will prepare chart papers mentioning the facts of closure property and the commutative property for rational numbers (a sample is given at the end). Instructions: The teacher will place the two bowls containing the chits on her table and will name it as Team 1 and Team 2. Both the teams will be given a working space on the board. Nothing will be a staned activity. The teacher will paste the chart on the board and draw a scoreboard for both the teams. In the teacher will paste the chart on the board (in their allotted space). The teacher will hen shrow the dice. If the upward face shows an arithmetic operator, for instance, '+' comes up, the two students will need to add the numbers that they both got within 90 seconds, i.e., they will add % and 11/3 in both the orders, i.e., 4/5 + 11/3 and 11/3 + 4/5. It. will be done similarly for all arithmetic operators. If the face shows- 'try again', then the two students will need to return their chits and go back to their seats. The next student from both the teams will then come and pick out a chit from their respective bowl, for instance, teat will intervere will fand 11/3 and 11/3 + 4/3. It. Wil | | |

| 7. 1 8. A th | The chits After all the scored | once used would not go back into the bo he chits have been exhausted, the teacher poard. | wls. will announce the winner as |
|--|---|---|---|
| The teach prepared | er will n for the c | ow engage the students in a discussion and losure and the commutative properties. | d bring their attention to the |
| The teach arithmetic | er will fi operation | rst discuss the closure property of rationa ons. | l numbers under the four |
| | | Closure Property of Rational nu | nbers |
| | S. No. | Statement | Yes/No |
| | 1 | On adding two rational numbers, we always get a rational number | |
| | 2 | On subtracting two rational numbers, we always get a rational number | |
| | 3 | On multiplying two rational numbers, we always get a rational number | |
| | 4 | On dividing two rational numbers, we | |
| The teach true for e done earli | er will ta ach oper | always get a rational number ake up statements in the given order, and v ration or not. The teacher would use the e | will discuss if the property ho examples taken from the activ |
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| The teach true for e done earli could refe Similarly, t teacher ar examples there isn't The comp | er will ta ach oper ier and h er to the the teach nd the st where th t any on oleted tab S. No. 1 2 | always get a rational number ake up statements in the given order, and y ration or not. The teacher would use the e ighlight it from the board directly. For inst addition sums done on the board. her could discuss the commutative proper- udents will simultaneously complete both he property is not satisfied. The teacher co the board during the discussion, if require oles would appear something like below: Closure Property of Rational nu Statement On adding two rational numbers, we always get a rational number On subtracting two rational numbers, we always get a rational number | will discuss if the property ho examples taken from the active cance, for statement I, the te ty. During the discussion, the the tables and provide non build give non- examples hers d. mbers Yes/No Yes Yes |
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| | Commutative Branarty of Pational | numbers |
|---------------------------|---|---|
| | | |
| S. No. | Statement | Yes/No |
| 1 | Addition is commutative for rational numbers, i.e., For any two rational numbers a and b , a + b = b + a | Yes |
| 2 | Subtraction is commutative for rational numbers, i.e., For any two rational numbers a and b , a - b = b - a | No $5 - \frac{3}{2} = \frac{7}{2}$ $\frac{3}{2} - 5 = \frac{-7}{2}$ |
| 3 | Multiplication is commutative for rational numbers, i.e., For any two rational numbers a and b , $a \times b = b \times a$ | Yes |
| 4 | Division is commutative for rational numbers, i.e., For any two rational numbers a and b , $a \div b = b \div a$ | No $5 \div 6 = \frac{5}{6}$ $6 \div 5 = \frac{6}{5}$ |
| Suggestion: The teacher c | ould do a similar exercise for th | e other properties. |



Objective: To represent rational numbers on a number line.

Materials required: Chits prepared by the teacher, notebooks, scale, pencils.

Preparation required by the teacher before the class:

• The teacher will need to prepare chits (in abundance) mentioning a rational number on each of them.

Instructions:

- This activity will be done in pairs. The students can do it with their partners.
- The teacher will place all the chits in a bowl on her table.
- One volunteer from each pair will come forward and randomly choose 10 chits each.
- The students will have to draw number line in their notebooks and represent those 10 rational numbers on it.
- The teacher will be there to handle queries of the students.

Further tasks after the students have represented the 10 rational numbers on the number line:

- Arrange the 10 rational numbers in ascending order.
- Did any two numbers represent the same number?
- The teacher could ask the teams to interchange their chits and repeat the whole process once again. This way each team will get a variety of examples.
- After the class is over, the students will return the chits to the teacher.

Sample chits are given below:

| ⁻²⁰ /35 | ⁹ /3 | ⁸ /5 | ¹² / ₃₆ | 0 | ⁻³ /9 |
|--------------------|------------------------------|--------------------|-------------------------------|------------------|------------------|
| -2/3 | ² / ₁₀ | 7 | -1.5 | ² /3 | ³ /9 |
| ⁻⁹ /3 | -2/3 | -12/ ₃₆ | -10/ ₁₅ | 11 _{/7} | ⁻⁵ /8 |

2. LINEAR EQUATIONS IN ONE VARIABLE

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|--|--|---|
| Meaning of Linear Equation in one variable and its solution | List the properties of algebraic expression and algebraic equation in order to differentiate between the two Identify the variable(s) and the highest power of the variable in a given algebraic equation in order to distinguish whether it is a linear equation in one variable or not Substitute the given values of variable in order to verify whether it is the solution of the equation or not | |
| Solving Equations which have Linear Expressions on one Side and Numbers on the other Side | Transpose terms to the other side in order to solve linear equations which have linear expression on one side and numbers on the other side | Use variables in order to solve puzzles and daily life problems |
| Applications of Linear Equations with one variable | Write simple contextual problems as linear equations in one variable in order to find its solution | |
| Solving Equations having the Variable on both Sides | Transpose terms to the other side in order to solve linear equations in one variable which have | |
| Reducing Equations to Simpler Form | Simplify the given linear equation in one variable in order to solve them | |
| Equations Reducible to the Linear Form | Use cross multiplication in order to reduce certain equations into their linear form | |

Test items



LOB: List the properties of algebraic expression and algebraic equation in order to differentiate between the two

I. A set of equations and expressions is given below: 2x, x + 5, 3x - 2 = 5, xyz + 5x + 3y, 2y + 5 = 0Which of the following options correctly represents the number of algebraic expressions and equations given in the set? **Option I:** Examples of algebraic expressions: 5 Examples of algebraic equations: 0 **Option 2:** Examples of algebraic expressions: 0 Examples of algebraic equations: 5 **Option 3:** Examples of algebraic expressions: 2 Examples of algebraic equations: 3 **Option 4:** Examples of algebraic expressions: 3 Examples of algebraic equations: 2 **Correct Answer:** Option 4 2. Consider the statements. Statement A: 3x + 5 is an example of algebraic expression because equality (=) sign is missing in it and it consists of variable, numbers, and operations. Statement B: 2x - 6 = 11 is an example of algebraic equation because it is an equality involving variables and has an equality sign. Which of these statement(s) is/are correct? **Option I:** Only Statement A

Option 2: Only Statement B Option 3: Both Statement A and Statement B Option 4: Neither Statement A nor Statement B Correct Answer: Option 3

LOB: Identify the variable(s) and the highest power of the variable in a given algebraic equation in order to distinguish whether it is a linear equation in one variable or not

I. Which of these equations is a linear equation in one variable?

Option 1: 2x + 5 = 14x **Option 2:** 2x + 5y = 14 **Option 3:** $2x^2 + 5 = 4$ **Option 4:** $\frac{2}{x} + 3x = 0$ **Correct Answer:** Option 1

 Consider the equation as shown. x^{m-3} + 15y²ⁿ⁻² = 2
 What should be the value of m and n such that the above equation is a linear equation in one variable?
 Option 1: m = 3, n = 3
 Option 2: m = 3, n = 1.5

```
Option 3: m = 4, n = 2
Option 4: m = 4, n = 1.5
Correct Answer: Option 2
```

LOB: Substitute the given values of variable in order to verify whether it is the solution of the equation or not

1. Which of these is a solution of the equation 2(x - 9) = -14? Option 1: x = 0Option 2: x = 1

Option 2: x = 1**Option 3:** x = 2

Option 4: x = 3**Correct Answer:** Option 3

2. Consider the equation shown below: 5x - a = 14; where a is any number Given that x = 4 is a solution of the equation, what is the value of a? Option 1: 3 Option 2: 6 Option 3: 9 Option 4: 18 Correct Answer: Option 2

LOB: Transpose terms to the other side in order to solve linear equations which have linear expression on one side and numbers on the other side

I. Which of these is the solution for the equation 3x + 13 = -8?

Option I: x = -7Option 2: x = 7Option 3: $x = \frac{5}{3}$ Option 4: $x = -\frac{5}{3}$ Correct Answer: Option I

2. What is the solution of the equation
$$\frac{7t-3}{5} + \frac{t+11}{10} = \frac{1}{10} - \frac{3}{5}$$
?
Option 1: $t = -\frac{3}{2}$
Option 2: $t = -\frac{2}{3}$
Option 3: $t = \frac{2}{3}$
Option 4: $t = \frac{3}{2}$
Correct Answer: Option 2

LOB: Write simple contextual problems as linear equations in one variable in order to find its solution

I. Anita has ₹1800 and saves ₹600 each week to buy a new guitar that costs ₹12000. If n represents the number of additional weeks, she needs to save to buy the guitar, which equation represents the situation and what will be the value of n?

Option 1: 1800 + 600*n* = 12000; *n* = 23 **Option 2:** 1800 + 600*n* = 12000; *n* = 17 **Option 3:** 1800*n* + 600 = 12000; *n* = 6 **Option 4:** 1800*n* + 600 = 12000; *n* = 7 **Correct Answer:** Option 2

2. Raman sells printed t-shirts and plane t-shirts at his shop. He sells each printed t-shirt for ₹350 and each plane t-shirt for ₹230. On a day, he sells a total of 50 t-shirts for ₹14260. How many of each kind of t-shirt has he sold on that day?

```
Option 1: Printed t-shirts = 35 and Plane t-shirts = 15
Option 2: Printed t-shirts = 15 and Plane t-shirts = 35
Option 3: Printed t-shirts = 27 and Plane t-shirts = 23
Option 4: Printed t-shirts = 23 and Plane t-shirts = 27
Correct Answer: Option 4
```

LOB: Transpose terms to the other side in order to solve linear equations in one variable which have variable on both the sides

1. What is the solution of the linear equation (4x - 5) - (2 + 3x) = (7x - 6)?

Option I: $x = -\frac{13}{8}$ Option 2: $x = -\frac{1}{8}$ Option 3: $x = -\frac{13}{6}$ Option 4: $x = -\frac{1}{6}$ Correct Answer: Option 4

2. Which of these is the solution of the equation $\frac{5u-3}{6} - \frac{3u+2}{3} = \frac{u}{6} - 3?$ Option 1: u = -12.5 Option 2: u = -5.5 Option 3: u = 5.5 Option 4: u = 12.5 Correct Answer: Option 3

E8M0207: Simplify the given linear equation in one variable in order to solve them

I. What is the solution of the linear equation 9k - 2(3 + 4k) = 3(2k - 1)?

Option 1: $k = -\frac{9}{7}$ Option 2: $k = -\frac{3}{5}$ Option 3: $k = \frac{3}{5}$ Option 4: $k = \frac{9}{7}$ Correct Answer: Option 2

- **2.** Which of these is the solution of the equation $3\left(\frac{x-5}{7}\right) 2\left(\frac{2x-11}{3}\right) = \frac{1}{21}[2(x+3) 5(x+1)]?$
 - Option I: $x = \frac{55}{8}$ Option 2: $x = \frac{54}{11}$ Option 3: $x = \frac{27}{4}$ Option 4: x = 5Correct Answer: Option 3

LOB: Use cross multiplication in order to reduce certain equations into their linear form

- 1. What is the solution of the equation $\frac{2x+1}{2x-1} = 2$? Option 1: $-\frac{3}{2}$ Option 2: $-\frac{2}{3}$ Option 3: $\frac{2}{3}$ Option 4: $\frac{3}{2}$ Correct Answer: Option 4
- 2. At a retail store, the cost of a plastic pot is ₹50 more than the cost of a broomstick. If the ratio of the cost of two pots to the cost of three broomsticks is 5:6, what is the cost of the pot?

Option 1: ₹150 Option 2: ₹200 Option 3: ₹250 Option 4: ₹300 Correct Answer: Option 3

Suggested Teacher Resources





Lesson Plan



| Objective | Write simple contextual problems as linear equations in one variable in order to find its solution. | | |
|-----------------------|--|--|--|
| Prerequisite | Linear equation in one variable and the methods to find its solution | | |
| Vocabulary words | Equation, solution, coefficients, variables. | | |
| Materials required | Chalk and blackboard, Pen/pencil and notebook. | | |
| Procedure | The teacher will begin by presenting a problem- | | |
| | Mrs. Ratna, the owner of a saree shop knows that there are 700 sarees in her shop but wants to reorganize how they are displayed on the counters. She needs to know how many cotton sarees; designer sarees and silk sarees are in the shop. She knows that the shop has four times as many cotton sarees as silk sarees and half as many designer sarees as cotton sarees. If these are the only types of sarees in the shop, how many of each type of saree are in the shop? | | |
| | The teacher will give 2-3 minutes to the students to work individually on the problem before initiating a discussion. The students will have to formulate an equation and then find its solution. | | |
| | In the given problem, there are basically 4 elements, i.e., cotton sarees, designer sarees, silk sarees and the total number of sarees. | | |
| | In the problem statement, we have been given the value of the total number of sarees. So, lets represent the total number of sarees by a long rectangle. | | |
| | 700 sarees | | |
| | We have been given that there are four times as many cotton sarees as silk sarees and number of designer sarees is half the number of cotton sarees. So, let us represent silk sarees, cotton sarees and designer sarees in terms of rectangles. Silk sarees: | | |
| | Designer sarees: | | |
| | This helps us in deciding that we should choose silk sarees as variable x because silk sarees have the fewest number in this case. Choosing a different type of saree would create fractions throughput the problem. | | |
| | So, if the number of silk sarees= x , Then, number of cotton sarees= $4x$ And, number of designer sarees= $2x$ If we again represent the situation in terms of rectangles, we get this | | |
| | 10 | | |

| | | 700 sarees | | |
|-----------|--|---|--|--|
| | x | 4 <i>x</i> | 2 <i>x</i> | |
| | Now, we can easily write an equation which represents the above table/diagram. | | | |
| | Taking x as th | he variable here, we can create a linear equation in one x + 4x + 2x = 700 | e variable as | |
| | Now to find t | the value of x, we need to solve this equation. 7x = 700 | | |
| | (dividing both | n sides by 7), $\frac{7x}{7} = \frac{700}{7}$ $x = 100$ | | |
| | The value <i>x</i> = Hence, the num And the num | = 100 here means that there are 100 silk sarees availab umber of cotton sarees = $4x = 4 \times 100 = 400$ ber of designer sarees = $2x = 2 \times 100 = 200$ | ble in the shop. | |
| | This way Mrs | s. Ratna's problem could be solved. | | |
| | The teacher of write an equa | could give different types of problems to the students v ation and then solve it. A suggestion is given below: | wherein they need to first | |
| | Nisha has 270 has three tim | 0 channels on her cable TV, Harsh has half the number les the number of channels as Atul, how many channels | of channels as Atul. If Nisha does Harsh have? | |
| | This problem we can denot | a could also be approached in a manner similar to Mrs. te the number of channels with Nisha and Harsh both i | Ratna's problem above. Here n terms of Atul's channels. | |
| | So, let us assu Number of cl | ume that the number of channels Atul has $= a$ hannels Harsh has $= a/2$ | | |
| | From the pro | nannels Nisna has = $3a$ oblem statement, we know that there are 270 channels represented by the equation given below: 3a = 270 | in Nisha's cable TV which | |
| | | (Dividing both sides by 3) $\frac{3a}{3} = \frac{270}{3}$ a = 90 | | |
| | Therefore, nu Number of cl Thus, there a | umber of channels Atul has= 90 hannels Harsh has= $\frac{a}{2} = \frac{90}{2} = 45$ are 45 channels on Harsh's cable TV. | | |
| Reference | https://www.e | engageny.org/ | | |



Objective: To solve a variety of linear equations in one variable.

Materials required: Blackboard, chalk, duster, 2 set of cards with linear equations in one variable written on them.

Preparation required:

- Select around 20 linear equations in one variable which you want the students to practice
- Prepare two cards for each equation.
- For example, for linear equation

4x + 10 = 3(x + 10)

Mention the expression given in LHS in the 1st card and the RHS in 2nd card. Both the cards should be numbered the same. That means, there will be two different cards with the same number but different linear expressions.

Like, there will be two cards numbered 5 but one of them will have 4x + 10 and the other 3(x + 10) written over it.

• After creating both sets of cards, shuffle them together.

Instructions:

- Put the shuffled cards in a bowl or a box and let each student randomly pick one card.
- Ensure that there are even number of students so that no student gets left out from the activity.
- After all the students have each got a card, tell the students to pair up with the person who has got the other card for the same number.
- The students along with their respective partners should solve the equation by equating the expressions given on their cards in their notebooks.
- The teacher should ideally not give more than 5 minutes for the students to solve and then take the cards back in the bowl or the box.
- Now the teacher should randomly pick out any card, check its number so that the team who solved it initially will now have to come to the blackboard and discuss their solution with the others.
- This exercise would then continue for other equations as well.

Note: the current content material is for 30 students but the teachers can always create more equations if there are more than 40 students.

| Number on card | Card I | Card 2 |
|----------------|-----------------------------------|---------------------|
| I | $\frac{a+1}{4}$ | $\frac{a-2}{3}$ |
| 2 | 0.50(8p-10) | 1.50 p + 16 |
| 3 | $\frac{9q+6}{6q-9}$ | $-\frac{9}{12}$ |
| 4 | $\frac{15y}{2y-1}$ | 6 |
| 5 | 4x + 10 | 3(x + 10) |
| 6 | 3x - 4 | 1 - 2x |
| 7 | 14b + 7 | -6 |
| 8 | 6h + 16 | 2h - 12 |
| 9 | 30t - 10 | 20t + 20 |
| 10 | 21 + <i>x</i> | 5x - 3(2x + 1) |
| 11 | $j - \frac{j-1}{2}$ | $1 - \frac{j-2}{3}$ |
| 12 | $\frac{12x-10}{4}$ | $\frac{6x+12}{4}$ |
| 13 | $\frac{3t-2}{3} + \frac{2t+3}{2}$ | $t + \frac{7}{6}$ |
| 14 | 4t - 3 - (3t + 1) | 5t - 4 |
| 15 | $\frac{2q-3}{4} - \frac{3q-5}{2}$ | $q + \frac{3}{4}$ |

Reference: https://www.educationworld.com/a_tsl/archives/07-1/lesson016.shtml

3. UNDERSTANDING QUADRILATERALS

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome | |
|--------------------------------|---|---|--|
| | List the properties of a polygon in order to classify the given figures as a polygon | | |
| Classification of Polygons | List the properties of different types of polygons in order to classify them as regular or irregular, concave or convex | | |
| | Recall the angle sum property of triangle in order to extend it for quadrilaterals | Use angle sum property in order to solve | |
| Angle sum property of polygons | Relate the angle sum property of triangle and quadrilateral in order to extend it for an n-sided polygon | problems related to angles of quadrilateral | |
| | Apply angle sum property of a quadrilateral in order to find the measure of the unknown angle in a given quadrilateral | | |
| Sum of the Measures of | Apply exterior angle property of a | | |
| the Exterior Angles of a | polygon in order to find the measure | | |
| Polygon | of the unknown angle in a given figure | | |
| Kind of Quadrilaterals | List the properties of quadrilaterals in order to classify them as trapezium, kite and parallelogram | | |
| | Discuss the properties of a parallelogram in order describe the relation between its opposite sides, angles and diagonals. | Apply reasoning through activities such as | |
| Some special Parallelograms | Discuss the properties of a rhombus in order to classify it as special case of kite and parallelogram | constructing parallelograms, drawing their diagonals and measuring their sides and angles in order to verify properties of parallelograms | |
| | Discuss the properties of a rectangle in order to show that it is a special case of parallelogram | | |
| | Discuss the properties of a square in order to show it as special case of parallelogram, rhombus and rectangle | | |

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2. From each vertex of a polygon, all diagonals are drawn. If exactly nine diagonals are drawn, which polygon is drawn?

Option 1: Heptagon Option 2: Pentagon Option 3: Hexagon Option 4: Octagon Correct Answer: Option 3

LOB: List the properties of different types of polygons in order to classify them as regular or irregular, concave or convex



- 2. A student draws a polygon. The properties of the polygon are as shown.
 - No diagonal lies in the exterior of the polygon.
 - The length of one of the sides is twice the length of another side.

Which of these polygons could the student have drawn?



LOB: Recall the angle sum property of triangle in order to extend it for quadrilaterals

I. Consider a quadrilateral PQRS shown.



Which expression represents the sum of the measures of all the angles of the quadrilateral PQRS? **Option 1:** $2 \times 90^{\circ}$ **Option 2:** $2 + 180^{\circ}$ **Option 3:** $2 \times 180^{\circ}$

Option 4: 2 + 90° **Correct Answer:** Option 3

2. Consider the quadrilateral ABCD below.



What is the measure of $\angle DAB$ of the quadrilateral ABCD?

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LOB: Apply angle sum property of a quadrilateral in order to find the measure of the unknown angle in a given quadrilateral

I. What is the measure of $\angle X$ in the quadrilateral WXYZ?



Option I: 101° **Option 2:** 248° **Option 3:** 259° **Option 4:** 281° Correct Answer: Option 1

2. Observe the quadrilateral below.



I. Ankita draws a quadrilateral with properties given below.

- Two pairs of parallel sides.
- Opposite sides and opposite angles are equal.

• Diagonals of quadrilateral bisect each other.

Which of these quadrilaterals she could have drawn?





2. Two students are determining in which quadrilateral the measure of all interior angles can be calculated, given the measure of one interior angle. Their response is as shown:
Student A: The quadrilateral will be kite.
Student B: The quadrilateral will be an isosceles trapezium.
Whose response is correct?
Option I: Only Student A
Option 2: Only Student B
Option 3: Both the students
Option 4: Neither student A nor B

Correct Answer: Option 2

LOB: Discuss the properties of a parallelogram in order describe the relation between its opposite sides, angles and diagonals.

I. Consider a parallelogram shown.



What is the measure of angle JML? Option 1: 70° Option 2: 110° Option 3: 125° Option 4: 140° Correct Answer: Option 1

2. Consider a parallelogram shown.



Given that the length of PR = 10 cm and SQ = 24 cm, what is the perimeter of the parallelogram PQRS? Option 1: 26 cm Option 2: 34 cm Option 3: 47 cm Option 4: 52 cm Correct Answer: Option 4

LOB: Discuss the properties of a rhombus in order to classify it as special case of kite and parallelogram

I. Consider a parallelogram CARD with one pair of known sides.



What additional information is required to make it a square?

Option I:

- The measure of $\angle P = 90^{\circ}$.
- One pair of equal adjacent sides.
- Diagonals of equal length and are perpendicular to each other.

Option 2:

- The measure of $\angle P = 90^\circ$.
- Diagonals of equal length.

Option 3:

- The measure of $\angle P = 60^{\circ}$.
- One pair of equal adjacent sides.
- Diagonals of equal length and are perpendicular to each other.

Option 4:

- One pair of equal adjacent sides.
- Diagonals are perpendicular to each other.

Correct Answer: Option 1

Suggested Teacher Resources

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Lesson Plan



| Objective | List the properties of a polygon in order to classify the given figures as a polygon | | |
|---------------------|--|--|--|
| Prerequisite | Line segments, curves, triangles | | |
| Vocabulary words | Polygons, Quadrilaterals, simple closed curves | | |
| Materials required | Blackboard, chalks, notebooks | | |
| Procedure | • The teacher will begin by drawing a set of examples and non-examples of polygons on the blackboard. A sample for the same has been given below. | | |
| | Example of Polygons Non-Examples A A | | |
| | not polygons. The students should be given time to observe and analyse the two sets and note down any similarities within the polygons set and any differences between the two sets and come up with their own definition of a polygon. | | |
| | 28 | | |

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The students will work in pairs and note down their observations. Some samples responses are given below:

- A few students might write about polygons using prior knowledge.
- A Few of them might write the differences between both of them by analysing their sides, nature of curves etc.
- In order to define the term 'Polygon', the teacher will draw the template (of the Frayer's model) on the blackboard on the clean side without rubbing the examples and non- examples of polygons.



- The students will make a similar table in their notebooks keeping the word 'Polygon' at the centre.
- The teacher will then engage the students in a discussion.

If the first set of figures (Polygons) is carefully observed, it could be seen that all the figures are closed figures whereas in set 2 not all figures are closed, some are open curves as well.

Another thing noticeable is that in set I (polygons) the curves do not cross each other even once hence they are simple closed curves whereas in set 2, we have such examples.

One major observation is that the figures in set 1 (polygons) are made up of only line segments only whereas the figures in set 2 show curved edges as well.

So, it could be said that any simple closed curve which is entirely made up of line segments (joined end to end), is a polygon.

- The students will have to fill in the table on their own based on the discussion
 - In the first part, the student will write the definition of Polygon in their own words.
 - In the second part, the students will write characteristics of polygons.
 - In the third part, students will give some examples of polygons.
 - In the fourth part, students will give some non- examples of polygons.
- The teacher will then summarize, and also fill in her version of the definition for the term 'polygon' on the board so that the students can cross check if they have noted down all the features of polygons.
- The teacher will then give examples of polygons with which the students are already familiar with like triangles, square, rectangle, hexagon, etc.
- The teacher will then show some more figures like below and ask the students to classify the given figures into polygons and non- polygons.



• Students should keep the definition of Polygons in front of them. The teacher should give a few minutes to the students for this task. Post which the teacher should ask volunteers about each figure one by one wherein volunteers have to give reasons of why the specific figure is a polygon or a non-polygon.

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Objective: To visualize the relation between the interior and the exterior angles in n-sided regular polygons (as the number of sides increases).

The teacher will need to arrange large cut-outs for regular polygons.

The teacher will also need sheets with different regular polygons pasted or printed on them to distribute to each student.



The teacher will begin by pasting a big chart paper on the board on which the cut-out of an enlarged equilateral triangle is pasted. She will engage the students in a discussion by asking a few questions as below. The students will be working on the sheets provided to them.

- Is this a regular polygon or an irregular polygon?
 - This is an Equilateral triangle. Hence it is a regular polygon.
- What can we say about the angles and sides of each of this polygon?
- The measure of each angle is equal and the length of each side is equal in a regular polygon.
- What is the angle sum of a triangle?
 - The sum of the interior angles of a triangle is 180°.
- What is the measure of each interior angle of an equilateral triangle?
 - The teacher will encourage the students to measure each interior angle of the equilateral triangle on the sheets provided to them. It will come out to be 60° each.
 - What is the sum of exterior angles of a polygon?
 - It is 360°.
- What is the measure of each exterior angle of an equilateral triangle?
 - The measure of each exterior angle of an equilateral triangle is 120°. The process done for interior angles will be repeated to measure the exterior angles.
- Now the teacher will take up a square, a regular pentagon and other regular polygons one by one and will repeat the same process as done for an equilateral triangle and record the measure of their interior and exterior angles.

| Number of sides of the | Measure of each interior | Measure of each exterior |
|------------------------|--------------------------|--------------------------|
| regular polygon | angle | angle |
| 3 | 60° | 120° |
| 4 | 90° | 90° |
| 5 | 108° | 72° |
| 6 | 120° | 60° |
| : | : | : |

| n | $(n-2) \times 180^{\circ}$ | 360° |
|---|----------------------------|------|
| | \overline{n} | n |

- It will be noted that as the number of sides increases,
 - the angle sum increases as per the formula $n-2 \times 180^\circ$, where n is the number of sides.
 - the measure of each interior angle increases
 - the measure of each exterior angle decreases
- It will be observed that a regular polygon with the
 - Maximum exterior angle possible is in an equilateral triangle where each exterior angle measures 120°.
 - Minimum interior angle possible is in an equilateral triangle where each interior angle measures 60°.
- It can be an extension to encourage the students to think that if we keep on increasing the number of sides for a regular polygon, we will get a circle at some point.

4. PRACTICAL GEOMETRY

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|---------------------------------|---|---|
| Constructing a Quadrilateral | Discuss and list the minimum number of elements required in order to construct a unique quadrilateral List and execute steps of construction in order to construct a quadrilateral given the length of its four sides and a diagonal List and execute steps of construction in order to construct a quadrilateral given the length of its three sides and two diagonals List and execute steps of construction in order to construct a quadrilateral given the length of two adjacent sides and measures of three angles are known List and execute steps of construction in order to construct a quadrilateral given the length of three sides and measures of two included angles are known | Use compasses and straight edge in order to construct a given quadrilateral |
| Some Special | Identify the minimum number of elements required in order | |
| Cases | to construct special cases of quadrilaterals | |

Test items LOB: Discuss and list the minimum number of elements required in order to construct a unique guadrilateral Which of the following options shows the minimum measurements required to construct a unique Ι. quadrilateral? **Option I:** Two adjacent sides and the included angle **Option 2:** Two adjacent sides and three angles **Option 3:** Four sides and two diagonals **Option 4:** Three sides and a diagonal **Correct Answer:** Option 2 2. A part of construction of a quadrilateral ABCD is shown. Which of the following options shows the minimum additional measurements required to construct the quadrilateral? Option I: AD and AC Option 2: AD and CD **Option 3:** AD, CD and $\angle A$ **Option 4:** AD, CD and $\angle C$ Correct Answer: Option 2 LOB: List and execute steps of construction in order to construct a quadrilateral given the length of its four sides and a diagonal

1. A part of construction of a quadrilateral PQRS where PQ = 4 cm, QR = 5 cm, RS = 7 cm, PS = 4.8 cm and PR = 2.5 cm is shown below.



Which of the following options shows the next two steps required to construct the quadrilateral PQRS?

Option I: Step I: Taking R as the centre and radius equal to 7 cm, draw an arc. **Step 2:** Taking P as the centre and radius equal to 4.8 cm, draw and arc intersecting the arc drawn in previous step at S. Join PR and RS to get quadrilateral PQRS.

Option 2: Step I: Taking P as the centre and radius equal to 7 cm, draw an arc. **Step 2:** Taking R as the centre and radius equal to 4.8 cm, draw and arc intersecting the arc drawn in previous step at S. Join PR and RS to get quadrilateral PQRS.

Option 3: Step I: Taking Q as the centre and radius equal to 7 cm, draw an arc.

Step 2: Taking R as the centre and radius equal to 4.8 cm, draw and arc intersecting the arc drawn in previous step at S. Join PR and RS to get quadrilateral PQRS.

Option 4: Step I: Taking R as the centre and radius equal to 7 cm, draw an arc.

Step 2: Taking Q as the centre and radius equal to 4.8 cm, draw and arc intersecting the arc drawn in previous step at S. Join PR and RS to get quadrilateral PQRS.

Correct Answer: Option I

2. Mrinal constructs a quadrilateral ABCD where AB = 11 cm, BC = 10 cm, CD = 8 cm, AD = 12 cm and diagonal AC = 6 cm.



Is his construction correct?

Option 1: No, because in triangle ABC; AB + BC > AC, AB + AC > BC, BC + AC > AB and in triangle ACD; CD + AD > AC, CD + AC > AD, AC + AD > CD.
Option 2: Yes, because in triangle ABC; AB + BC > AC, AB + AC > BC, BC + AC > AB and in triangle ACD; CD + AD > AC, CD + AC > AD, AC + AD > CD.
Option 3: No, because AB + BC + AC < AD + CD + AC.
Option 4: Yes, because AB + BC + AC < AD + CD + AC.
Correct Answer: Option 2

LOB: List and execute steps of construction in order to construct a quadrilateral given the length of its three sides and two diagonals

I. The first three steps to construct a quadrilateral WXYZ where XY = 9 cm, WZ = 11 cm, YZ = 10 cm, diagonal WY = 11 cm and diagonal XZ = 14 cm are listed below.
Step 1: Draw WY = 11 cm.
Step 2: Taking Y as the centre and radius equal to 10 cm, draw an arc.
Step 3: Taking W as the centre and radius equal to 11 cm, draw an arc intersecting the arc drawn in step 2 at Z. Join WZ and YZ.
Which option correctly shows the next two steps required to complete the construction?

Option 1: Step 4: Taking Y as the centre and radius equal to 14 cm, draw an arc opposite to Z. Step 5: Taking Z as the centre and radius equal to 9 cm, draw an arc intersecting the arc drawn in step 4 at X. Join WX, XY and XZ to get the required quadrilateral WXYZ.
Option 2: Step 4: Taking W as the centre and radius equal to 9 cm, draw an arc opposite to Z. Step 5: Taking Z as the centre and radius equal to 14 cm, draw an arc opposite to Z. Step 5: Taking Z as the centre and radius equal to 14 cm, draw an arc intersecting the arc drawn in step 4 at X. Join WX, XY and XZ to get the required quadrilateral WXYZ.
Option 3: Step 4: Taking Y as the centre and radius equal to 9 cm, draw an arc opposite to Z. Step 5: Taking Z as the centre and radius equal to 9 cm, draw an arc opposite to Z.
Option 3: Step 4: Taking Y as the centre and radius equal to 14 cm, draw an arc intersecting the arc drawn in step 4 at X. Join WX, XY and XZ to get the required quadrilateral WXYZ.
Option 4: Step 4: Taking W as the centre and radius equal to 14 cm, draw an arc opposite to Z.
Step 5: Taking Z as the centre and radius equal to 14 cm, draw an arc intersecting the arc drawn in step 4 at X. Join WX, XY and XZ to get the required quadrilateral WXYZ.

- Correct Answer: Option 3
- 2. Anamika constructs a quadrilateral ABCD where BC = 18 cm, AD = 22 cm, CD = 20 cm, diagonal AC = 22 cm and diagonal BD = 28 cm.



Which of the following options justifies that her construction is correct? **Option 1:** AC = AD **Option 2:** BC + AD + CD > AC + BD Option 3: In triangle BCD; BC + CD ≠ BD, CD + BD ≠ BC, BD + BC ≠ CD and in triangle ACD; AC + AD ≠ CD, AC + CD ≠ AD, CD + AD ≠ AC Option 4: In triangle BCD; BC + CD > BD, CD + BD > BC, BD + BC > CD and in triangle ACD; AC + AD > CD, AC + CD > AD, CD + AD > AC
Correct Answer: Option 4

LOB: List and execute steps of construction in order to construct a quadrilateral given the length of two adjacent sides and measures of three angles are known

Question Text: A teacher asked her students to construct a quadrilateral ABCD with AB = 12 cm, BC = 9 cm, ∠A = 60°, ∠B = 105° and ∠C = 105°. A student performed the following steps of construction.
 Step 1: Draw AB = 12 cm.
 Step 2: Taking B as the centre, draw ∠ABE = 105°.

Step 3: Taking A as the centre and radius equal to 9 cm, draw an arc intersecting BE at C.

Step 4: Taking A as the centre, draw \angle BAF = 105°. **Step 5:** Taking C as the centre, draw \angle BCG = 60°.

The student made an error while constructing the quadrilateral. In which step did the student make the first error?

Option 1: Step 2 Option 2: Step 3 Option 3: Step 4 Option 4: Step 5 Correct Answer: Option 2

2. Richa constructed a quadrilateral PQRS based on the information given to her.



Option 1: Measures of PQ, QR, ∠P, ∠Q and ∠R Option 2: Measures of PQ, QR, ∠P, ∠Q, ∠R and ∠S Option 3: Measures of PQ, QR, RS, PS and PR Option 4: Measures of PQ, QR, RS, PS and QS Correct Answer: Option 1

LOB: List and execute steps of construction in order to construct a quadrilateral given the length of three sides and measures of two included angles are

1. A part of construction of a quadrilateral ABCD where AB = 11 cm, BC = 16 cm, CD = 9 cm, $\angle B = 60^{\circ}$ and $\angle C = 105^{\circ}$ is shown below.



Which of these options shows the next three steps to complete the construction? **Option 1:** Step 4: Taking B as the centre and radius equal to 11 cm, draw an arc intersecting BE at A.
Step 5: Taking C as the centre and radius equal to 9 cm, draw an arc intersecting CF at D. Step 6: Join AD to get the required quadrilateral ABCD.

Option 2: Step 4: Taking B as the centre and radius equal to 9 cm, draw an arc intersecting BE at A. Step 5: Taking C as the centre and radius equal to 11 cm, draw an arc intersecting CF at D. Step 6: Join AD to get the required quadrilateral ABCD.

Option 3: Step 4: Taking F as the centre and radius equal to 11 cm, draw an arc intersecting BE at A.

Step 5: Taking E as the centre and radius equal to 9 cm, draw an arc intersecting CF at D. Step 6: Join AD to get the required quadrilateral ABCD.

Option 4: Step 4: Taking F as the centre and radius equal to 9 cm, draw an arc intersecting BE at A. Step 5: Taking E as the centre and radius equal to 11 cm, draw an arc intersecting CF at D. Step 6: Join AD to get the required quadrilateral ABCD.

Correct Answer: Option 1

2. The steps to construct a quadrilateral WXYZ where WX = 7 cm, XY = 9 cm, YZ = 12 cm, $\angle X = 105^{\circ}$ and $\angle Y = 75^{\circ}$ in a random order are as follows.

Step I: Draw XY = 9 cm.

Step 2: Taking Y as the centre, draw $\angle XYS = 75^{\circ}$.

Step 3: Taking X as the centre and radius equal to 7 cm, draw an arc intersecting XT at W.

Step 4: Taking X as the centre, draw \angle YXT = 105°.

Step 5: Taking Y as the centre and radius equal to 12 cm, draw an arc intersecting YS at Z.

Step 6: Join WZ to get the required quadrilateral WXYZ.

Which two steps should be interchanged so that the construction becomes possible?

Vinay: Step 3 and Step 4

Chetan: Step 3 and Step 5

Who is/are correct?

Option 1: Only Vinay Option 2: Only Chetan Option 3: Both Vinay and Chetan Option 4: Neither Vinay nor Chetan Correct Answer: Option 3

LOB: Identify the minimum number of elements required in order to construct special cases of quadrilaterals

I. What is the minimum number of elements required to construct a unique rectangle?

Option 1: One Option 2: Two Option 3: Three Option 4: Four Correct Answer: Option 2

2. Nikhil has to draw a quadrilateral in which each pair of the consecutive sides is congruent, but the opposite sides are not congruent. What is the minimum number of elements will he require to construct the quadrilateral?

Option 1: One Option 2: Two Option 3: Three Option 4: Four Correct Answer: Option 3

Suggested Teacher Resources



Lesson Plan



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| Objectives | List and execute steps of construction in order to construct a quadrilateral given the length of its four sides and a diagonal. |
|---------------------------|--|
| Prerequisite Knowledge | How to use a compass and a scale. |
| Material Required | Chalk and Blackboard, A Big sized compass preferably from the Math lab for the teacher (to be able to demonstrate the construction on board) Pen/Pencil and notebook. Compass and scale for students. |
| Procedure | Start the class by drawing a rough quadrilateral on the board. For instance, draw a square PQRS. Start the class by drawing a rough quadrilateral on the board. For instance, draw a square PQRS. Discuss that a quadrilateral has ten parts in all: four sides, four angles and two diagonals. In square PQRS, i. Four sides: PQ, QR, RS and SP ii. Four angles: $\angle P$, $\angle Q$, $\angle R$ and $\angle S$. In this case all angles are right angles. iii. Two diagonals: PR and QS Note: The teacher could take any general quadrilateral for the above discussion as well. To construct a quadrilateral, we need the measures of five specified. These are: i. When the length of four sides and a diagonal are given ii. When the length of two diagonals and three sides are given iii. When the length of three sides and measures of three angles are given and, iv. When the length of three sides and the measures of two angles between them are given. The measures given should also satisfy the properties: Triangle inequality and the angle sum property of a quadrilateral. Only then the quadrilateral given could be drawn. In addition, to these four cases, special cases of parallelograms could be constructed with information of less than five measurements. |
| | Now the teacher could begin by discussing the first case and focus on the construction of a quadrilateral when we are given the length of four sides and one diagonal and demonstrate this construction using a compass, scale and chalk on the board. |
| | j sample quesuon: |

Construct a quadrilateral ABCD in which AB = 4.8 cm, BC = 4.3 cm, $\overline{CD} = 3.6$ cm, AD = 4.2cm and diagonal AC = 6 cm. It could be seen that here we have got five measures, i.e. Four sides and one diagonal. Before the actual construction, the rough figure is to be constructed. Drawing a rough figure helps in avoiding mistakes during construction. 3.6 cm С 6 cm 4.2 cm 4.3 cm 4.8 cm R Now, we could see that the given quadrilateral ABCD satisfies the triangle inequality. In $\triangle ABC$ $\ln \Delta ADC$ AB + BC > ACAD + DC > ACBC + AC > ABDC + AC > ADAC + AB > BCAD + AC > DCSo now, the teacher would demonstrate the construction step by step on the board. Steps of Construction: **Step I**: Since we have been given the length of all four sides, we can start the construction by taking any one of the four sides as the base. For instance, we will start the construction by taking AB as the base, i.e., Draw AB = 4.8 cm by using a scale. **Step 2**: Now, since we have started with AB, the \triangle ABC should be constructed first. We will have to locate the point C. We have been given that AC= 6cm, so using a compass and scale take a radius equal to 6cm and with A as center, draw an arc. Step 3: With B as center and radius equal to 4.3 cm, draw another arc which intersects the previous arc drawn from point A. Name this point of intersection as C. **Step4:** Join AC and BC. We have now constructed the $\triangle ABC$. **Step 5**: Now we have to construct $\triangle ADC$. We know that AD=4.2cm is given so, with A as center and radius equal to 4.2 cm, draw an arc. Step 6: We know that DC= 3.6cm is given so, with C as center and radius equal to 3.6 cm, draw another arc, which intersects the previous arc at point D. **Step 7**: Join AD and CD. Thus, ABCD is the required quadrilateral. C 0 3.6 Cm 4.8cm Note: The teacher would be required to note down the steps of construction on board. i. The usage of the tools of construction at each step is to be carefully explained during ii. the demonstration.





5. DATA HANDLING

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|-------------------------------|---|--|
| Looking for Information | Recall the different types of graphical representation (namely pictograph, bar graph and double bar graph) of data in order to represent the given data in the most suitable representation and interpret them | |
| Organising raw data | Use tally marks in order to organise the given raw data in a frequency distribution table | |
| | Use tally marks in order to prepare a grouped frequency distribution table for large ungrouped data | Draw and interpret bar graphs and pie charts |
| Grouping data | Construct histogram in order to represent the given grouped data | based on them |
| | Discuss the elements of the given histogram in order to interpret it | |
| Circle graph or Pie Chart | List and execute steps of construction in order to construct a circle graph Read a given circle graph in order to infer a variety | |
| | of information from it | Conduct activities in order to makes |
| Chance and | order to define the equally likely outcomes | hypotheses on chances of future events on |
| Probability | List all the possible outcomes of an event in order to calculate the probability of a given event | the basis of its earlier occurrences or available data like, after repeated throws of dice and coins |

Test items



LOB: Recall the different types of graphical representation (namely pictograph, bar graph and double bar graph) of data in order to represent the given data in the most suitable representation and interpret them

I. Which of these can be represented by a double bar graph?

Option I: The marks obtained by a student in different subjects of an exam.

Option 2: The number of visitors entering a museum every hour from 10 am to 5 pm.

Option 3: The percentage of budget allocated to different departments of an office.

Option 4: The number of girls and boys in different classes of a school.

Correct Answer: Option 4

2. Which of these graphs will be the best measure to represent the marks obtained by 5 students in two Mathematics tests and why?

Option 1: Bar graph; because it shows the relationship or comparison among discrete categories.
Option 2: Double bar graph; because it shows the relationship or comparison among two groups.
Option 3: Bar graph; because it shows the frequency of data divided into equal groups.
Option 4: Double bar graph; because it shows the frequency of data divided into equal groups.

Correct Answer: Option 2

LOB: Use tally marks in order to organize the given raw data in a frequency distribution table

1. Question Text: Consider the data collected from students of a class to choose the language they prefer to study.

French, German, Spanish, Sanskrit, German, German, French, French, Spanish, Sanskrit, French, Sanskrit, Spanish, German, French, German, German, Sanskrit, German, Sanskrit, Spanish, German, French, German, French, German, Sanskrit, Spanish

Which of these tables correctly represents the given data?

| | Languages | Number of Students |
|-----------|-----------|--------------------|
| | French | TH TH |
| | German | 111 M |
| | Spanish | Ĩ |
| Option I: | Sanskrit | ₩ II |
| · | Languages | Number of Students |
| | French | M III |
| | German | THI THI |
| | Spanish | 1HU II |
| Option 2: | Sanskrit | ₩I |
| • | Languages | Number of Students |
| | French | 11 III |
| | German | THI THI |
| | Spanish | ₩I |
| Option 3: | Sanskrit | 1₩1 II |
| | Languages | Number of Students |
| | French | M M |
| | German | 1HL III |
| | Spanish | 1HL II |
| Option 4: | Sanskrit | 1HL |
| | | |

- 2. A study was conducted to determine the favourite sports of 20 students of a class. The results are:
 - Cricket is the favourite sport of most students
 - Football is the least favourite sport among students
 - Badminton is more liked by the students than Basketball

Based on the given information, which of these can be the correct tally marks representing the given data?

| | Sports | Number of Students |
|------------------------|--|---|
| | Badminton | THU I |
| | Cricket | 1HU II |
| | Basketball | |
| Option I: | Football | |
| | Sports | Number of Students |
| | Badminton | 1¥U II |
| | Cricket | THI I |
| | Basketball | |
| Option 2: | Football | 1111 |
| | | |
| | Sports | Number of Students |
| | Sports Badminton | Number of Students |
| | Sports Badminton Cricket | Number of Students Null Null |
| | Sports Badminton Cricket Basketball | Number of Students >>> >>>> >>>> >>>> >>>> |
| Option 3: | Sports Badminton Cricket Basketball Football | Number of Students |
| Option 3: | Sports Badminton Cricket Basketball Football Sports | Number of Students >>> >>>> >>>> >>>> >>>> >>>> >>> >>> >>> Number of Students |
| Option 3: | Sports Badminton Cricket Basketball Football Sports Badminton | Number of Students ``+`` |
| Option 3: | Sports Badminton Cricket Basketball Football Sports Badminton Cricket | Number of Students >>> >>>> >>>> >>>> >> >> >> >> >> >> >> >> >> >> >> >> >> >> >> >> |
| Option 3: | Sports Badminton Cricket Basketball Football Sports Badminton Cricket Basketball | Number of Students >>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >> >> >> >> >> >> >> >> >> >> >> >> >> |
| Option 3: Option 4: | Sports Badminton Cricket Basketball Football Badminton Cricket Basketball Football | Number of Students ™ ™ III IIII Number of Students IIII IIII IIII IIII |

LOB: Use tally marks in order to prepare a grouped frequency distribution table for large ungrouped data

Consider the time taken (in seconds) by 30 students of a class to finish a 100 m race.
 17.39, 16.50, 18.10, 17.20, 18.55, 19.45, 15.55, 15.20, 17.45, 19.20, 16.30, 18.58, 16.45, 18.30, 16.38, 16.45, 18.35, 16.52, 17.45, 17.20, 19.20, 16.40, 15.10, 15.40, 19.50, 18.20, 16.20, 16.58, 18.50, 19.58, 16.30
 Which of these tables correctly represents the given data?

| | Time Taken (in seconds) | Number of Students |
|------------------|--|---|
| | 15 - 16 | |
| | 16 - 17 | THI THI |
| | 17 - 18 | τ× |
| | 18 - 19 | ™ II |
| Option I: | 19 - 20 | ₩I |
| | | |
| | Time Taken (in seconds) | Number of Students |
| | Time Taken (in seconds) 15 - 16 | Number of Students |
| | Time Taken (in seconds) 15 - 16 16 - 17 | Number of Students |
| | Time Taken (in seconds) 15 - 16 16 - 17 17 - 18 | Number of Students |
| | Time Taken (in seconds) 15 - 16 16 - 17 17 - 18 18 - 19 | Number of Students \\\\\ \\\\\ \\\\\ \\\\\ \\\\\ \\\\\ \\\\\ \\\\\ \\\\\ |

| | Time Taken (in seconds) | Number of Students |
|-----------|--|---|
| | 15 - 16 | 1111 |
| | 16 - 17 | TH TH |
| | 17 - 18 | THL I |
| | 18 - 19 | 1HU I |
| Option 3: | 19 - 20 | 144 |
| - | | |
| | Time Taken (in seconds) | Number of Students |
| | Time Taken (in seconds) 15 - 16 | Number of Students |
| | Time Taken (in seconds) 15 - 16 16 - 17 | Number of Students |
| | Time Taken (in seconds) 15 - 16 16 - 17 17 - 18 | Number of Students |
| | Time Taken (in seconds) 15 - 16 16 - 17 17 - 18 18 - 19 | Number of Students >>> >>> >>> >>> >>> >>> >>> >>> >>> |

Correct Answer: Option 1

- 2. Sheena collected the data to find the average time spent by an employee to commute to the office with 25 employees. She finds that:
 - highest number of employees take less than 60 minutes to commute
 - fewest number of employees take more than 90 minutes to commute
 - there are fewer number of employees who take less than 30 minutes to commute than the number of employees who take 60 minutes or more but less than 90 minutes.

Which of these tables correctly represents the data?

| | Time Taken (in seconds) | Number of Employees |
|------------------|--|--|
| | 0 - 30 | |
| | 30 - 60 | 141 III |
| | 60 - 90 | |
| Option I: | 90 - 120 | |
| | Time Taken (in seconds) | Number of Employees |
| | 0 - 30 | |
| | 30 - 60 | |
| | 60 - 90 | 1₩I IIII |
| Option 2: | 90 - 120 | 111 |
| | Time Taken | |
| | (in seconds) | Number of Employees |
| | (in seconds) | Number of Employees |
| | (in seconds) 0 - 30 30 - 60 | Number of Employees Number of IIII Number of Employees |
| | (in seconds) 0 - 30 30 - 60 60 - 90 | Number of Employees NH IIII NH NH III III |
| Option 3: | (in seconds) 0 - 30 30 - 60 60 - 90 90 - 120 | Number of Employees Number of Intervention Number of Intervention |
| Option 3: | (in seconds) 0 - 30 30 - 60 60 - 90 90 - 120 Time Taken (in seconds) | Number of Employees >>> >>>> >>>> >>>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> >>> Number of Employees |
| Option 3: | (in seconds) 0 - 30 30 - 60 60 - 90 90 - 120 Time Taken (in seconds) 0 - 30 | Number of Employees Number of Employees Number of Employees II |
| Option 3: | (in seconds) 0 - 30 30 - 60 60 - 90 90 - 120 Time Taken (in seconds) 0 - 30 30 - 60 | Number of Employees >>> >>>> >>>> >> >> >> >> >> >> >> >> >> >> >> >> >> >> >> >> >> >> |
| Option 3: | (in seconds) 0 - 30 30 - 60 60 - 90 90 - 120 Time Taken (in seconds) 0 - 30 30 - 60 60 - 90 | Number of Employees \mathcal{H} |

Correct Answer: Option 2

LOB: Construct histogram in order to represent the given grouped data

1. The average salary package taken by students of a recent batch of 30 students in a college is as shown.

| Annual salary package (in Lakh | ns) Number of Students |
|--------------------------------|------------------------|
| 3-5 | 2 |
| 5-7 | 6 |
| 7-9 | 12 |
| 9-11 | 8 |
| | |

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2. Consider the information for the number of calls received by a customer care executive between 11 am to 5 pm.

- most of the calls were received in the last hour of the day
- there are two instances in which the number of calls received per hour was the same
- No call was received in between 1 pm to 2 pm.

Based on the given information, which of these graphs correctly represents the data?



LOB: Discuss the elements of the given histogram in order to interpret it

I. The histogram below shows the age of the participants in a play.



How many participants are below the age of 25 years? Option 1: 10 Option 2: 8 Option 3: 6 Option 4: 4 Correct Answer: Option 2

2. The histogram shown below represents the number of vehicles passing through a toll bridge each hour on a particular day.



Which of these is true about the given histogram?

Option I: the number of vehicles passing through the toll before 3 pm is 50% of the number of vehicles passing through the toll after 3 pm

Option 2: the number of vehicles passing through the toll before 2 pm is 50% of the number of vehicles passing through the toll after 2 pm.

Option 3: the number of vehicles passing through the toll before 2 pm is equal to the number of vehicles passing through the toll after 2 pm

Option 4: the number of vehicles passing through the toll before 3 pm is equal to the number of vehicles passing through the toll after 3 pm

Correct Answer: Option 2

LOB: List and execute steps of construction in order to construct a circle graph

I. The table below shows different pets and the number of students that own the pet.

| Pets | Number of Students |
|---------|--------------------|
| Dog | 12 |
| Cat | 8 |
| Hamster | 3 |
| Rabbit | 5 |

Akhil wants to represent the data in a circle graph, where each sector of the graph represents number of students that own a pet. Which of these is not a step to construct a circle graph?

Option I: Find the total number of students.

Option 2: Find the fraction or percentage that each sector represents.

Option 3: Finding the degree the central angle of each sector.

Option 4: Finding the area of each sector.

Correct Answer: Option 4

2. The table below shows the number of different flowers sold by a florist on a day.

| Flowers | Number of Flowers Sold |
|----------|------------------------|
| Rose | 30 |
| Tulip | 10 |
| Hibiscus | 15 |
| Lilly | 25 |

Akriti represents the data on a circle graph in which each sector represents the number of sales of the flowers. Which of these represents the angle of each sector?

| Sector | Angle |
|--------|-------|
| Rose | 135° |
| | |

| Tulip | 45° |
|-----------|--------|
| Hibiscus | 67.5° |
| Lilly | 112.5° |
| Option 2: | |
| Sector | Angle |
| Rose | 135° |
| Tulip | 45° |
| Hibiscus | 112.5° |
| Lilly | 67.5° |
| Option 3: | |
| Sector | Angle |
| Rose | 45° |
| Tulip | 135° |
| Hibiscus | 67.5° |
| Lilly | 112.5° |
| Option 4: | |
| Sector | Angle |
| Rose | 45° |
| Tulip | 135° |
| Hibiscus | 112.5° |
| Lilly | 67.5° |

Correct Answer: Option I

LOB: Read a given circle graph in order to infer a variety of information from it

1. The circle graph below shows the dance forms preferences of 300 students of a school.



How many students prefers to learn Bharatanatyam? Option 1: 84 Option 2: 36 Option 3: 48 Option 4: 16 Correct Answer: Option 3

2. The data was collected to determine the mode of transport used by employees of an office as shown.



If 66 people commute by bus, how many more employees prefers to commute by metro than car? **Option 1:** 600 **Option 2:** 276

Option 3: 165

Option 4: 150 Correct Answer: Option 4

LOB: List all the possible outcomes of an experiment in order to deduce that each of the outcomes has the same chance of occurring

I. A bag has 3 identical black balls marked with Alphabets A to C on it. If two balls are selected at random, which of these shows the possible outcomes?

Option 1: {AB, AC, BA, BC, CA, CB, AA, BB, CC} Option 2: {AB, BC, CA} Option 3: {AB, AC, BA, BC, CA, CB} Option 4: {A, B, C} Correct Answer: Option 3

2. Two spinners each divided into three sectors such that each sector is marked with number 1 to 3. The sample space is:

{11,12,13,21,22,23,31,32,33} Consider the conditions below. Condition 1: Each sector must be equal in area. Condition 2: Spinners should be identical. Which of these is required to prove that each outcome is equally likely? Option 1: Only Condition 1 Option 2: Only Condition 2 Option 3: Both Condition 1 and 2 Option 4: Neither Condition 1 nor Condition 2 Correct Answer: Option 3

LOB: List all the possible outcomes of an event in order to calculate the probability of a given event

1. Jagat has 15 cards marked with 1 to 15 on it. Which of these is the list of all possible outcomes of getting a card with a number divisible by 3?

Option 1: {3, 6, 9, 12} Option 2: {3} Option 3: {3, 6, 9, 12, 15} Option 4: {5, 10, 15} Correct Answer: Option 3

2. A bag contains some identical balls. Out of those, 45% are blue, 30% are yellow and rest are red in colour. If a ball is picked at random, what is the probability that it is not a red ball?

Option I: $\frac{1}{4}$ Option 2: $\frac{3}{4}$ Option 3: $\frac{1}{3}$ Option 4: $\frac{2}{3}$ Correct Answer: Option 2

Suggested Teacher Resources



Lesson Plan



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| Objectives | Construct histogram in order to represent the given data in a graph. | | | |
|---------------------------|--|---|--------------------------|--------------------------|
| Prerequisite Knowledge | Knowledge of Tally marks, frequency, scale and intervals. | | | |
| Material Required | Graph paper. | | | |
| Time Required | 45 minutes | | | |
| Procedure | Start the class with th students- | e following real-life proble | em to test the pre-re | quisite knowledge of the |
| | Frequency Table w | ith Intervals | | |
| | The boys' and girls' basketball teams at your School wanted to raise money to help buy new uniforms. They decided to sell baseball caps with the school logo to family members and other interested fans. To obtain the correct cap size, students had to measure the head circumference (distance around the head) of the adults who wanted to order a cap. The following data set represents the head circumferences, in millimetres (mm), of the adults. 513, 525, 531, 533, 535, 535, 542, 543, 546, 549, 551, 552, 552, 553, 554, 555, 560, 561, 563, 563, 565, 565, 568, 568, 568, 571, 571, 574, 577, 580, 583, 583, 584, 585, 591, 595, 598, 603, 612, 618 The caps come in six sizes: XS, S, M, L, XL, and XXL. Each cap size covers an interval of head circumferences for each cap size. The interval 510- 530 represents head circumferences from 510 mm to 530 mm, not including 530. | | | |
| | Cap Sizes | Interval of Head Circumferences (millimetres) | Tally | Frequency |
| | XS | 510 - 530 | | |
| | S | 530 - 550 | | |
| | M | 550 - 570 | | |
| | L | 570 - 590 | | |
| | XL | 590 - 610 | | |
| | XXL | 610 - 630 | | |
| | Now ask the students | to complete the followin | g table. It will look so | omething like this- |
| | | 49 | | |

| Cap Sizes | Interval of Head Circumferences (millimetres) | Tally | Frequency |
|-----------|---|---------------------------|-----------|
| ×s | 510-530 | Ш | 2 |
| S | 530-550 | ### 111 | 8 |
| М | 550-570 | IIII IIII IIII | 15 |
| L | 570-590 | +++ 111 | 9 |
| XL | 590-610 | 1111 | 4 |
| XXL | 610-630 | II | 2 |

Now help the students to construct a histogram using the following instructions-To make a histogram:

- Draw a horizontal line (x axis), and mark the intervals.
- Draw a vertical line (y axis), and label its Frequency.
- Mark the Frequency axis with a scale that starts at 0 and goes up to few levels up which are greater than the largest frequency in the frequency table.
- Draw a jagged line or broken line (it means, we are not showing the number between 0 and 510)
- on the x axis and start marking head circumference starting from 510 till the highest given head circumference with suitable given interval.
- For each interval, draw a bar over that interval that has a height equal to the frequency for that interval.

Demonstrate by drawing the first two bars of the histogram -



Now ask the students to complete the Histogram. It will look something like this



- 1. Teacher starts the activity by discussing the Corona pandemic, causes, symptoms, toll on the entire world etc.
- Teacher will then take the students to the computer lab and will ask them to surf the given information over web and complete the task: Take the data of top 5 countries which are most affected by corona till 31st March 2020. Make 3 different histograms depicting the information mentioned below for each country:

i) Number of People affected by the virus.

ii) Number of people died.

iii)Number of people recovered.

Choose an appropriate scale to construct the histograms.

Follow Up Question:

Combine all the above three graphs with suitable scale. And represent all the three lines with different colours.

6. SQUARES AND SQUARE ROOTS

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|----------------------------|---|----------------------------|
| | Define perfect squares in order to classify the given numbers as | |
| | perfect squares or non-perfect squares | |
| | Observe the number in order to find the unit place of its square | |
| Properties of | Observe different number patterns in order to deduce square | |
| Square Numbers | numbers | |
| 1 | Use the rule that there are exactly 2n non-perfect square numbers | |
| | between the squares of the number n and $(n+1)$ in order to find | |
| | how many numbers, lie between the squares of the given two | |
| | consecutive numbers | |
| Finding the | Use the rule that a perfect square number (n^2) can be written as | |
| Square of a | the sum of first n odd natural numbers in order to distinguish | |
| Number | between square and non-square numbers | |
| | Ose Pythagoras theorem in order to find the Pythagorean triplet | |
| | Apply inverse operations on a given perfect square in order to | |
| | deduce square root of this number | Apply different methods in |
| | Ose method of repeated subtraction in order to find the square | order to find the squares |
| | Use prime factorization method in order to find the square root of | cubes, square roots and |
| | the given perfect square | cube roots of a given |
| | Use prime factorization method in order to determine whether | number |
| | the given number is a perfect square or not | |
| | Use prime factorization method in order to find the smallest | |
| Square Roots | number to be operated (all the four arithmetic operations) on | |
| | given number to get a perfect square and then find the square root | |
| | of the new number | |
| | Use long division method in order to find the square root of the | |
| | given perfect square number | |
| | Use long division method in order to find the smallest number to | |
| | be operated (all the four arithmetic operations) on given number | |
| | to get a perfect square and then find the square root of the new | |
| | number | |
| Square Roots of | Use long division method in order to find the square root of the | |
| Decimals | given decimal number | |
| Estimating | Use estimation in order to approximate the value of the square | |
| Square Root | root of the given number to the nearest whole | |



- **2.** The digit at unit's place of a square of a number is 2 more than the digit at unit place of that number. Which of these can be the digit at the unit's place of the square of the number?
 - Option 1: 1 Option 2: 3 Option 3: 5 Option 4: 9 Correct Answer: Option 4

LOB: Observe different number patterns in order to deduce square numbers

I. Which of these will give a square number?

Option I: Option 2: Option 3: Option 4: Correct Answer: Option 3 2. Consider a pattern shown. $4^2 = 16$ $34^2 = 1156$ $334^2 = 111556$ $3334^2 = 11115556$ Which of these will never be a part of the pattern? $33334^2 = 1111155556$ 333334² = 111111555556 **Option I:** 3333334² = 11111115555556 333334² = 111111555556 $3333334^2 = 11111115555556$ **Option 2:** 33333334² = 1111111155555556 3333334² = 11111115555556 $33333334^2 = 1111111155555556$ **Option 3:** 333333334² = 111111111555555556 $33333334^2 = 1111111155555556$ $333333334^2 = 111111111555555556$ **Option 4:** 3333333334² = 1111111115555555556 **Correct Answer:** Option 4

LOB: Use the rule that there are exactly 2n non perfect square numbers between the squares of the number n and (n+1) in order to find how many numbers, lie between the squares of the given two consecutive numbers

I. How many non-perfect square numbers lie between 8² and 9²?

```
Option 1: 15
Option 2: 16
Option 3: 18
Option 4: 19
Correct Answer: Option 2
```

- 2. Consider the three consecutive numbers *a*, *b* and *c*. If there are 54 non-perfect square numbers between *a* and *b*, how many non-perfect square numbers lie between the numbers *b* and *c*?
 - Option 1: 54 Option 2: 56 Option 3: 58 Option 4: 59 Correct Answer: Option 2

LOB: Use the rule that a perfect square number (n^2) can be written as the sum of first n odd natural numbers in order to distinguish between square and non-square numbers

I. Which of these can be expressed as the sum of first 8 odd natural numbers?

```
Option 1: 4<sup>2</sup>
Option 2: 8<sup>2</sup>
Option 3: 9<sup>2</sup>
Option 4: 16<sup>2</sup>
Correct Answer: Option 2
```

2. Consider the expression below. 1+3+5+7.....+(2k+1), where k is a natural number Which of these options describes the given expression? Option 1: The sum of the given expression is (k + 1)². Option 2: The sum of the given expression is (k - 1)². Option 3: The sum of the given expression is k². Option 4: The sum of the given expression is (2k + 1)².
Correct Answer: Option 1

LOB: Use Pythagoras theorem in order to find the Pythagorean triplet

If one member of the Pythagorean triplet is 10, which of these are the remaining members of the triplet?
 Option 1: 3 and 8
 Option 2: 6 and 8
 Option 3: 18 and 19
 Option 4: 35 and 36

- Correct Answer: Option 2
- 2. The product of the numbers 14 and 16 is determined by $using(p + 1)(p 1) = p^2 1$, where p is one of the members of the Pythagorean triplet which is neither the largest nor the smallest. Which of the following represents all the members of the Pythagorean triplet?

Option 1: 4, 15 and 17 Option 2: 8, 15 and 17 Option 3: 14, 15 and 16 Option 4: 8, 63 and 64 Correct Answer: Option 2

LOB: Apply inverse operations on a given perfect square in order to deduce square root of this number

I. What is the square root of 144? Option 1: 6 Option 2: 12 Option 3: 24 Option 4: 72 Correct Answer: Option 2

2. An integer k is obtained by multiplying a number c by itself. Consider the two statements about the square root of k.

Statement I: The square root of k is c if c > 0. Statement II: The square root of k is -c if c < 0. Which of these statements is correct? **Option 1:** Only Statement I **Option 2:** Only Statement II **Option 3:** Both Statements I and II **Option 4:** Neither Statement I nor II **Correct Answer:** Option 3 LOB: Use method of repeated subtraction in order to find the square root of the given square number

- I. Some steps to find the square root of a number are shown below.
 - 49 1 = 48
 - 48 3 = 45
 - 45 5 = 40
 - 40 7 = 33
 - 33 9 = 24
 24 || = |3
 - 13 13 = 0
 - 13 13 = 0

```
What is the square root of the number?

Option 1: 7

Option 2: 13

Option 3: 25

Option 4: 49
```

```
Correct Answer: Option I
```

2. The steps to determine the square root of a number *m* are shown below.

LOB: Use prime factorization method in order to find the square root of the given perfect square

```
1. The prime factorisation of a number is as shown.
2 × 2 × 3 × 3 × 3 × 3
What is the square root of the number?
Option 1: 6
Option 2: 8
Option 3: 18
Option 4: 22
Correct Answer: Option 3
```

2. A number d is such that it's prime factorisation consists of 12 prime numbers. Which of these shows the prime factorisation of the square root of the number?

LOB: Use prime factorization method in order to determine whether the given number is a perfect square or not

Which of these is a prime factorisation of a square number?
Option 1: 2 × 3 × 5 × 5
Option 2: 3 × 3 × 4 × 4 × 5 × 5
Option 3: 2 × 2 × 3 × 5 × 5 × 7 × 7
Option 4: 2 × 2 × 3 × 3 × 5 × 5 × 11 × 11

Correct Answer: Option 4

2. The prime factorization of an even square number is as shown. 3×3×5×5×7×7×7×p
What is the smallest value of p?
Option 1: 2
Option 2: 4
Option 3: 14
Option 4: 28
Correct Answer: Option 4

LOB: Use prime factorization method in order to find the smallest number to be operated (all the four arithmetic operations) on given number to get a perfect square and then find the square root of the new number

I. Which number should be multiplied by 108 such that it becomes a perfect square number?

Option 1: 2 Option 2: 3 Option 3: 5 Option 4: 6 Correct Answer: Option 2

2. A number *n* is written as $p^2q^4r^3$, where *p*, *q* and *r* are the prime factors. Which expression represents a perfect square number and what is the square root of the number?

Option I: $\frac{p^2q^4r^3}{r}$ and $\sqrt{\frac{p^2q^4r^3}{r}} = pq^2r$

Option 2:
$$\frac{p \cdot q}{p}$$
 and $\sqrt{\frac{p \cdot q}{p}} = pq^2r$

Option 3: $p^2q^4r^3 \times p$ and $\sqrt{p^2q^4r^3 \times p} = p^2q^2r$

Option 4:
$$p^2q^4r^3 \times q$$
 and $\sqrt{p^2q^4r^3 \times q} = pq^2r$

Correct Answer: Option I

LOB: Use long division method in order to find the square root of the given perfect square number

I. A part of work to find the square root of 1089 is shown below.

$$3 \overline{\begin{array}{c} 3 \\ \hline 1 \\ -9 \end{array}}$$

Which of the following shows the next step?

Option I:
$$32$$

 $3\frac{1089}{-9}$
 $92\frac{189}{-184}$
5



2. The length and breadth of a rectangular field are 80 m and 39 m respectively. What is the length of the diagonal of the field, by using the long division method?

Option I: 11 m Option 2: 55 m Option 3: 89 m Option 4: 97 m Correct Answer: Option 3

LOB: Use long division method in order to find the smallest number to be operated (all the four arithmetic operations) on given number to get a perfect square and then find the square root of the new number

- I. What is the least number that must be subtracted from 1170 to get a perfect square?
 - Option 1: 9 Option 2: 14 Option 3: 34 Option 4: 64 Correct Answer: Option 2
- 2. A square number is added to 2976 to make it a perfect square. What are the square roots of the square number that is added and the perfect square that is formed?

Option 1: 7, 55 Option 2: 7, 54 Option 3: 12, 56 Option 4: 12, 55 Correct Answer: Option 1

LOB: Use long division method in order to find the square root of the given decimal number

I. Which of these shows the square root of 53.29?

$$\begin{array}{c}
7.5 \\
7 \overline{53.29} \\
-49 \\
75 \overline{429} \\
-375 \\
54
\end{array}$$
Option I:



2. The diagonals of a rhombus are 6.6 m and 11.2 m. What is the side length of the rhombus?
 Option 1: 2.9 m
 Option 2: 4.3 cm
 Option 3: 6.5 m

Option 4: 8.9 m Correct Answer: Option 3

LOB: Use estimation in order to approximate the value of the square root of the given number to the nearest whole

I. What is the estimated square root of 750? Option I: 27

Option 2: 28 Option 3: 35 Option 4: 37 Correct Answer: Option 1

What is the greatest number whose estimated square root is 17?
 Option 1: 273
 Option 2: 289
 Option 3: 306
 Option 4: 307
 Correct Answer: Option 3

Suggested Teacher Resources



Lesson Plan



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| Objectives | Define perfect square in order to classify given number as perfect squares or non-perfect squares. | | | |
|---------------------------|--|-----|------------------|-----------|
| Prerequisite Knowledge | Multiplication and division | | | |
| Material Required | Chart paper | | | |
| Procedure | Teacher will give small pieces of paper cut in square shape to the group of 4 students. Teacher will then display a table depicting the side of a square and the number of square pieces used to make that particular square. Then we will ask students to calculate how many square pieces it takes them to make the pattern of the given side of a square. Table will look like this. | | | |
| | Side of a Square | | No. of square pi | eces used |
| | I | | I | |
| | 2 | | 4 | |
| | 3 | | 9 | |
| | 4 | | 16 | |
| | Questions to be asked -: I. How is the number of square pieces related to its side of the square? Identify the pattern. 2. Can you find the side of a square if it has 26 pieces of square? Follow up questions: After students understand the concept then give the following question to solve-: | | | |
| | Find the length of the pool if its area is 100 m^2? Check whether 121 is perfect or no perfect square. Create a perfect square table till 13. Expected Outcome: | | | |
| | Students will be able to understand the concept of perfect and non-perfect squares and square root numbers | | | |
| | Assessment: A society collected Rs 9216. Each number collected as many Rs as there were members. How many members were there and how much did each contribute? Find which one is perfect or non-perfect squares. | | | |
| | 25 | 37 | 144 | 300 |
| | 500 | 225 | 289 | 48 |
| | | - | <u> </u> | |



Objective: Students will be able to calculate the square and square roots of the numbers **Material Required**: Activity Sheet-Square Root Maze



Time Required -: 40 Mins-:

Instructions-:

- 1. Teacher will divide the students into groups of 4.
- 2. Each group will be given one activity sheet and a token.
- 3. Each group will put their token at the starting point of their sheet. Their task will be to start from the starting point and keep on solving the square root so as to move their token to the finish line of the activity sheet.
- 4. Teacher will hold a timer for each group. The group which reaches the finish point first will win.

Follow up questions-:

- I. Which of the following is a square of an even number?
 - a. 144 b.169 c.441 d.62
- 2. Add the square of 12 and 5 and then find the square root of it.
- 3. Sum of squares of natural numbers from 1 to 20.

Source: Chalk lit application and Pinterest

7. CUBES AND CUBE ROOTS

QR Code:



Learning outcome and Learning Objectives:

| Content area / | Learning Objectives | Learning Outcome | |
|-------------------|--|--|--|
| Concepts | | | |
| | Define perfect cube/cube number in order to classify the given numbers as cube numbers or non-cube numbers | | |
| | Observe the pattern of cube of even numbers in order to generalise that cubes of even numbers are even | | |
| | Observe the pattern of cube of numbers with one's digit as | | |
| | I, 2, 3, 4 etc. in order to explore the one's digit of their | | |
| | perfect cubes and comment on it | | |
| Cubes | Add n consecutive odd numbers in order to get the sum | | |
| | equal to n^3 | Apply different methods in order to find | |
| | Use prime factorization in order to rule out a number as a | the squares, cubes, square roots and | |
| | perfect cube | cube roots of a given number | |
| | Use prime factorization on the given number in order to | | |
| | find the smallest number to be operated (all the four | | |
| | arithmetic operations) on given number to get a perfect | | |
| | cube | | |
| | Use prime factorization in order to find the cube root of a | | |
| Cuba Poots | given number | | |
| | Use estimation in order to find the cube root of a given | | |
| | perfect cube | | |

Test items



LOB: Define perfect cube/cube number in order to classify the given numbers as cube numbers or non-cube numbers

I. Is 343 a perfect cube?

Option 1: Yes, because 3 is in one's place.
Option 2: No, because it is an odd number.
Option 3: No, because the sum of the digits is not a perfect cube.
Option 4: Yes, because all its prime factors can be grouped in triples.
Correct Answer: Option 4

2. Consider the given set of numbers.

{215, 625, 841, 1000, 1331, 2744, 12321, 27000, 35937, 64000}

Which option correctly classifies the given numbers as cube numbers and non-cube numbers?

Option I: There are 6 cube numbers and 4 non-cube numbers in the given set.

Option 2: There are 5 cube numbers and 5 non-cube numbers in the given set.

Option 3: There are 4 cube numbers and 6 non-cube numbers in the given set.

Option 4: There are 3 cube numbers and 7 non-cube numbers in the given set.

Correct Answer: Option I

LOB: Observe the pattern of cube of even numbers in order to generalize that cubes of even numbers are even

- Observe the pattern shown below.
 8, 64, 216, 512, ...
 Based on the pattern, which statement is true?
 Option 1: Cubes of all odd numbers are odd.
 Option 2: Cubes of all even numbers are even.
 Option 3: Cubes of all odd numbers end only in 1, 3, 5 and 7.
 Option 4: Cubes of all even numbers end only in 2, 4, 6 and 8.
 - **Correct Answer:** Option 2
- 2. If c is an even number, which statement is correct about the value of the expression $[c + (c + 2) + (c + 4) + (c + 6) + ...]^3$?

Option I: For any value of *c*, the value of the expression will be an odd number.

Option 2: For any value of *c*, the value of the expression will be a prime number.

Option 3: For any value of *c*, the value of the expression will be an even number.

Option 4: For any value of *c*, the value of the expression will be an irrational number.

Correct Answer: Option 3

LOB: Observe the pattern of cube of numbers with one's digit as 1, 2, 3, 4, etc. in order to explore the one's digit of their perfect cubes and comment on it

I. Which digit comes in one's place in the cube of 17325483?

```
Option 1: 1
Option 2: 3
Option 3: 7
Option 4: 9
Correct Answer: Option 3
```

Which digit comes in one's place in the result of the expression (21476 + 31520 + 41305 + 50697)³?
Option 1: 2 because 6 + 0 + 5 + 7 = 18 and 8 × 8 × 8 = 512
Option 2: 2 because 2 + 3 + 4 + 5 = 14 and 4 + 4 + 4 = 12
Option 3: 4 because 2 + 3 + 4 + 5 = 14 and 4 × 4 × 4 = 64
Option 4: 4 because 6 + 0 + 5 + 7 = 18 and 8 + 8 + 8 = 24

Correct Answer: Option I

LOB: Add n consecutive odd numbers in order to get the sum equal to n^3

I. How many consecutive odd numbers must be added to get the sum equal to 243?

Option 1: 2 Option 2: 4 Option 3: 20 Option 4: 24 Correct Answer: Option 4

2. Which of the following expressions can be used to find the value of [(43 + 45 + 47 + 49 + 51 + 53 + 55) - (31 + 33 + 35 + 37 + 39 + 41)]?

Option 1: | × 6 × 5 + 3 Option 2: | × 6 × 5 × 3 Option 3: | × 7 × 6 + 3 Option 4: | × 7 × 6 × 3 Correct Answer: Option 4

LOB: Use prime factorization in order to rule out a number as a perfect cube

I. Which of the following expressions will not yield a perfect cube?

Option 1: 2 × 2 × 2 × 3 × 3 × 3 Option 2: 4 × 4 × 4 × 4 × 4 × 4 × 5 × 5 × 5 Option 3: 6 × 6 × 6 × 6 × 6 × 3 × 3 × 3 × 3 Option 4: 8 × 8 × 8 × 4 × 4 × 4 × 5 × 5 × 5 × 5 × 5 × 5 Correct Answer: Option 3

Nimish claims that -1728 is not a perfect cube number. Which of the following options justifies his claim?
 Option 1: Nimish's claim is incorrect because each prime factor of -1728 appears three times.
 Option 2: Nimish's claim is correct because 8 is in one's place which is not divisible by 3.
 Option 3: Nimish's claim is incorrect because 1 + 7 + 2 + 8 = 18 which is divisible by 3.
 Option 4: Nimish's claim is correct because -1728 is a negative integer.
 Correct Answer: Option 1

LOB: Use prime factorization on the given number in order to find the smallest number to be operated (all the four arithmetic operations) on given number to get a perfect cube

- I. Which smallest number should be multiplied to 2592 so that the product is a perfect cube?
 - Option 1: 2 Option 2: 3 Option 3: 12 Option 4: 18 Correct Answer: Option 4
- 2. If $k = (m \times n)^4$ where m and n are the prime factors of k, which expression will result in a perfect cube nearest to k with only factors m and n?

Option I: $k \div (m \times n)$ Option 2: $k + (m \times n)$ Option 3: $k \times (m \times n)^2$ Option 4: $k - (m \times n)^2$ Correct Answer: Option 1

LOB: Use prime factorization in order to find the cube root of a given number

I. Which of the following options correctly shows the cube root of 13824?

Correct Answer: Option 3

2. If s and m are two perfect cube numbers such that $s = (a \times b)^6$ and $m = \frac{s}{8}$, which expression can be used to represent the cube root of m?

Option I: $\frac{ab}{2}$ Option 2: $\frac{ab}{4}$ Option 3: $\frac{(ab)^2}{2}$ Option 4: $\frac{(ab)^2}{4}$ Correct Answer: Option 3

LOB: Use estimation in order to find the cube root of a given perfect cube

I. What is the estimated cube root of 50653?

Option 1: 37 Option 2: 50 Option 3: 53 Option 4: 65 Correct Answer: Option 1

2. What is the cube root of 857375?

Option I: Cube root of 857375 is 85 because 8 is the leftmost digit and 5 is the rightmost digit in 857375.

Option 2: Cube root of 857375 is 98 because 8 is the greatest digit in 857375 and $9^3 < 857 < 10^3$. **Option 3:** Cube root of 857375 is 95 because 5 is the unit digit in 857375 and $9^3 < 857 < 10^3$. **Option 4:** Cube root of 857375 is 75 because both 5 and 7 are repeated in 857375.

Correct Answer: Option 3

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Suggested Teacher Resources



Lesson Plan



| Objective | Prime factorise a given number in order to find the smallest number to be operated (all the four arithmetic operations) on given number to get a perfect cube. | |
|---------------------|--|----------------------------|
| Prerequisite | Prime factorisation, Multiplication and division | |
| Vocabulary words | Prime factorization | |
| Materials required | Cubical blocks of side I unit | |
| Procedure | Teacher will introduce the cube root topic with the help of an activity of making a cube with the help of cubical blocks of side 1 unit. Teacher will divide the group accordingly with the given resources and the class strength. Each group will be given cube blocks and they have to make two to three different cubes with the help of those cubical blocks. Most of the students will be able to make a cube consisting of 8 and 27 cubical blocks. Then we will ask them to write its side(number of cubical blocks on one side) on the left column and its number of cube blocks used to make it on the right column. The table will look like this: | |
| | Cube of the Side | No. of cubical blocks used |
| | 2units | 8 |
| | 3units | 27 |
| | Students will be able to conclude that the meaning of a cube is multiplying the number itself three times. | |



Objective: Students will be able to calculate the cubes and cube roots of the numbers Material Required: Number Wheel



Time Required: 45 minutes Instructions:

- I. Teacher will present the number wheel in front of the class and divide the students in 12 groups.
- 2. Each group will come and spin the wheel. Group will find the cube of the number which will be indicated by the arrow after the spin.
- 3. Teacher will hold a timer for each group. The group which find the cube earliest, will win.

Follow Up Questions:

- I. Write cubes of all-natural numbers between I and 20 and verify the following statements:
 - a) Cubes of all odd natural numbers are odd
 - b) Cubes of all even natural numbers are even
- 2. Write cubes of 5 natural numbers which are multiples of 3 and verify the following:

'The cube of natural number, which is a multiple of 3 is a multiple of 27'

8. COMPARING QUANTITIES

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|----------------------------|--|--|
| Recalling Ratios and | Convert ratios to percentage in order to solve | |
| Percentages | the given questions | |
| | Apply the formula for discount and discount | |
| | percentage in order to solve the given problem | |
| Discount Profit Loss | on discount | |
| | Calculate the discount in given situations in | |
| | order to comment whether the seller has made | |
| | a profit/loss in the given transaction | |
| | Define and compare simple interest and | |
| Simple Interest and | compound interest in order to comment on the | |
| Compound Interest | situations where either of the two are applied | |
| Compound interest | Calculate the simple interest in order to find the | |
| | total amount to be paid by the debtor | Observe a given context in order to |
| | Use formula of simple interest in order to | apply the concepts of profit and loss, |
| Doducing a Formula for | deduce the formula to calculate the compound | discount, VAT, simple and compound |
| | interest | interest |
| Compound interest | Calculate the compound interest in order to find | |
| | the total amount to be paid by the debtor | |
| Pata Compounded | Define the terms 'compounded annually', | |
| Annually or Half Yearly | 'compounded half yearly' and 'compounded | |
| | quarterly' and give examples in order to | |
| | differentiate between the three | |
| | Use formula of compound interest in order to | |
| Applications of | solve problems related to increase (or decrease) | |
| | in population | |
| Formula | Use formula of compound interest in order to | |
| i oi mula | solve problems related to increase (or decrease) | |
| | in the price of an item in intermediate years | |





LOB: Convert ratios to percentage in order to solve the given questions

- 1. Which percentage is equivalent to $\frac{18}{25}$?
 - Option 1: 18% Option 2: 36% Option 3: 72% Option 4: 78% Correct Answer: Option 3
- 2. The table below shows the marks scored by Anuj in different subjects.

| Subject | Marks scored | Total Marks |
|-------------|--------------|-------------|
| English | 22 | 25 |
| Science | 52 | 60 |
| Hindi | 55 | 100 |
| Mathematics | 68 | 75 |

Of the marks given, in which subject he scored the highest percentage of marks? Option 1: Hindi Option 2: English Option 3: Science Option 4: Mathematics Correct Answer: Option 4

LOB: Apply the formula for discount and discount percentage in order to solve the given problem on discount

I. The marked price of a bottle is ₹100 and the discount percent is 25%. What is the sale price of the bottle? Option 1: ₹125

Option 2: ₹105 Option 3: ₹75 Option 4: ₹25 Correct Answer: Option 3

2. The table below shows the total marked price of the books of different sections that Ria bought.

| Genre | Marked Price (in |
|-----------|------------------|
| | ₹) |
| Science | ₹1500 |
| Horror | ₹1850 |
| Biography | ₹500 |

If there is a discount of 28% on all the sections of books, what is the total amount that she has to pay? Option 1: ₹1078 Option 2: ₹962.50 Option 3: ₹2772

Option 3: <2/72 Option 4: ₹2887.50 Correct Answer: Option 3

LOB: Calculate the discount in given situations in order to comment whether the seller has made a profit/loss in the given transaction

I. The cost of making two tables is ₹4,500. A store owner marked the price of each table as ₹2,500 and sold each table at a discount 2%. Which of these is correct about the given situation?
Ontion I: The store owner gave a discount of ₹100 on both the tables and incurred loss of ₹100.

Option 1: The store owner gave a discount of $\gtrless 100$ on both the tables and incurred loss of $\gtrless 100$.

Option 2: The store owner gave a discount of ₹50 on both the tables and incurred loss of ₹400.
 Option 3: The store owner gave a discount of ₹50 on both the tables and incurred profit of ₹100.
 Option 4: The store owner gave a discount of ₹100 on both the tables and incurred profit of ₹400
 Correct Answer: Option 4

- A shopkeeper bought 10 machines for ₹7,50,000 from a wholesale store. He marked the price of each machine as ₹80,000. If he sold each machine after a discount of 10%, which of these statements is correct?
 Option 1: The shopkeeper has made a loss of ₹30,000 after selling the machines.
 - **Option 2:** The shopkeeper has made a loss of ₹80,000 after selling the machines.
 - **Option 3:** The shopkeeper has made a profit of ₹30,000 after selling the machines.
 - **Option 4:** The shopkeeper has made a profit of ₹80,000 after selling the machines.

Correct Answer: Option 1

LOB: Define and compare simple interest and compound interest in order to comment on the situations where either of the two are applied

1. Arvind borrows a sum of₹2,50,000 at 6% p.a. simple interest for 3 years. On the same day, Asif borrows the same sum on the same rate of interest but compounded annually for 3 years. Who pays more interest and by how much?

Option 1: Asif will have to pay ₹2,754 more than Arvind as interest.
 Option 2: Asif will have to pay ₹7,454 more than Arvind as interest.
 Option 3: Arvind will have to pay ₹2,754 more than Asif as interest.
 Option 4: Arvind will have to pay ₹7,454 more than Asif as interest.
 Correct Answer: Option 1

2. Adil borrowed ₹4,00,000 from his friend Ankur at 5% per annum simple interest for 1 year 6 months. Had Adil borrowed this sum from a bank at 8% per annum compounded annually for 3 years, what extra amount would Adil have to pay?

Option 1: The extra amount that Adil have to pay is ₹30,000.
Option 2: The extra amount that Adil have to pay is ₹33,568.
Option 3: The extra amount that Adil have to pay is ₹45,557.40.
Option 4: The extra amount that Adil have to pay is ₹73,884.80.
Correct Answer: Option 4

LOB: Calculate the simple interest in order to find the total amount to be paid by the debtor

I. Arun lend ₹2,88,000 to his friend at the rate of 12% for 9 months. How much interest will he get?

Option 1: ₹25,920 Option 2: ₹34,560 Option 3: ₹3,11,040 Option 4: ₹3,13,920 Correct Answer: Option 1

Akash borrowed ₹18,000 at the rate of 3% p.a. for the first three years, 6% p.a. for the next two years and 9% p.a. for the period beyond five years. How much amount does Akash has to pay at the end of 7 years?
 Option 1: ₹7,020

Option 2: ₹10,980 Option 3: ₹25,020 Option 4: ₹33,980 Correct Answer: Option 3

LOB: Use formula of simple interest in order to deduce the formula to calculate the compound interest

I. A principal gives ₹3,200 as simple interest at the rate of 10% p.a. in 2 years. What will be the compound interest at the rate of 5% p.a. for 3 years on the same principal?

Option 1: ₹800 Option 2: ₹2,522 Option 3: ₹18,522 Option 4: ₹25,056

Correct Answer: Option 2

- 2. The simple interest on a certain sum of money for 3 years at 5% per annum is ₹540. Which of these is the compound interest on that sum at the same rate for the same period?
 - Option 1: ₹56745 Option 2: ₹98245 Option 3: ₹312545 Option 4: ₹416745 Correct Answer: Option 1

LOB: Calculate the compound interest in order to find the total amount to be paid by the debtor

 Prakash borrows a sum of ₹35,000 at 5% per annum compounded annually for 24 months. How much amount will he pay?

Option 1: ₹1750 Option 2: ₹3587.50 Option 3: ₹37895 Option 4: ₹38587.50 Correct Answer: Option 4

2. What will be the amount of ₹35,000 after 2 years 6 months, compounded annually, the rate of interest being 2% per annum during the first year, 5% per annum during the second year and 1.5% per annum during the last 6 months of the period?

Option 1: ₹13930.40 Option 2: ₹35894.80 Option 3: ₹37766.14 Option 4: ₹187860.80 Correct Answer: Option 3

LOB: Define the terms 'compounded annually', 'compounded half yearly' and 'compounded quarterly' and give examples in order to differentiate between the three

1. The table below shows 4 formulas to calculate compound interest.

| Formula A | C. I. = $P\left[\left(1 + \frac{r}{100}\right)^{2n} - 1\right]$ |
|-----------|--|
| Formula B | C. I. = $P\left[\left(1 + \frac{r}{100}\right)^n - 1\right]$ |
| Formula C | C. I. = $P\left[\left(1 + \frac{r}{400}\right)^{4n} - 1\right]$ |
| Formula D | C. I. = $P\left[\left(1 + \frac{r}{200}\right)^{\frac{n}{2}} - 1\right]$ |

If 'p' is the principal amount, 'r' is the rate of interest and 'n' is the number of years, which formula can be used to calculate compound interest, when compounded annually?

- Option 1: Formula A Option 2: Formula B Option 3: Formula C Option 4: Formula D Correct Answer: Option 2
- **2.** Akash wants to calculate the compound interest on $\mathfrak{F} x$ for *n* years at r% p.a. He uses the formula

 $x\left[\left(1+\frac{r}{100}\right)^n-1\right]$ to calculate the compound interest.

If n is replaced by 4n and 100 by 400, which of these is true?

Option I: Interest is compound monthly

Option 2: Interest is compound quarterly

- **Option 3:** Interest is compound half-yearly
- **Option 4:** Interest is compound annually

Correct Answer: Option 2
- LOB: Use formula of compound interest in order to solve problems related to increase (or decrease) in populationI. The population of a town was 50,000 in the year 1980. If the population of the town increased at a rate of
 - 12% each year, what is the estimated population of the town after 3 years?

Option 1:35,123 Option 2:59,550 Option 3:70,246 Option 4:72,235 Correct Answer: Option 3

2. The population of a small town was 1,16,000 on the last day of the year 1959. During the next year it increased by 8.5% but due to swine flu it decreased by 10% in the following year. What was its population at the end of the year 1961?

Option 1: 2,726 Option 2:59,550 Option 3:1,13,274 Option 4:1,18,726 Correct Answer: Option 3

LOB: Use formula of compound interest in order to solve problems related to increase (or decrease) in the price of an item in intermediate years

1. A machine was purchased 3 years ago at $\forall x$ and its value depreciated by 10% per annum. If its present value is $\forall 1,21,743$, what is the value of x?

Option 1: 91,467 Option 2:1,62,039 Option 3:1,67,000 Option 4:1,81,006 Correct Answer: Option 3

2. The cost of an electronic gadget was ₹1,45,000 at the beginning of 1993. In the beginning of the year 1994 the price was hiked by 2%. But due to the decrease in demand, the cost was reduced by 5% in the beginning of the year 1995. What was the cost of the item in 1995?

Option 1: ₹1,34,850 Option 2: ₹1,39,350 Option 3: ₹1,40,505 Option 4: ₹1,40,650 Correct Answer: Option 3

Suggested Teacher Resources



Lesson Plan



| Objective | Calculate the simple interest in order to find the total amount to be paid. | |
|-----------------------|--|--|
| Prerequisite | Ratio, Selling Price, Cost Price and Percentage | |
| Vocabulary words | Ratio, percentage | |
| Materials required | Toys of different market objects like car, furniture, bike etc. | |
| Procedure | Teacher will divide all the students into 3 groups. Each group will have I bank manager who will provide the loan and 4 shopkeepers having different products like cars, furniture, bikes, T.V etc. Ask each shopkeeper to decide the cost of each article. Ask the bank manager to decide the time period as for how long he can give a particular loan and decide the rate of interest as well. Each shopkeeper will go to any of the bank managers to ask for the loan. Shopkeepers can go to more than one manager in order to fetch the minimum rate of interest on the loan amount. Then the teacher will tell the class the amount they got from the bank is their Principal. The duration in which they have to return the amount to the bank is the Time Period and the Interest. Then the teacher will introduce the formula of Simple Interest =(P X R X T)/100. Ask students to calculate their Interest and ask them how much money they will have to give to the bank manager at the end. Then the students will derive the Amount by the formula on their own i.e. Amount = Principal + Interest. Follow-Up Discussion: Have you ever heard about loans? Have you ever seen any loan related hoardings around? Find out various kinds of loans which banks give to customers and their rate of interests also. | |



Objective: This small-group game will help students to identify the numeric values for the principal, rate, and interest located in word problems.

Material Required:

- Sets of cards with word problems written on them
- Chart paper

• Markers

Instructions:

- 1. Prior to the game, the teacher will create sets of cards with word problems involving simple interest written on them. Give each word problem a number.
- 2. Teacher will provide the class with a real-life scenario involving simple interest, such as interest in a savings account or a consumer loan.
- 3. Then, she will discuss the formula for simple interest and identify the different variables, such as I (interest), P (principal), R (rate), and T (time).
- 4. She will divide the class into teams, and provide each team with chart paper, markers, and a set of the word problem cards you made.
- 5. Each team should divide their chart paper into columns for the variables P, R, and T. Also, they should create a column for the number of each word problem card.
- 6. When the teacher says, 'go,' the teams will read each word problem and categorize the numbers in the word problems under the correct variable on their chart paper.
- 7. Students will write the number written on the word problem card and then write the numbers from the word problem that correspond to each variable.

For example, in the word problem:

45,000Rs is deposited into a savings account. After one year,4 months and 20 days it totals 52,500Rs. Calculate the simple interest rate for this account.

Students are expected to label 45,000Rs as P, One Year 4 months and 20 days as T and 52,500Rs as the amount. They need to determine the simple interest.

8. The first team to correctly categorize the variables from their word problems wins.

Discussion:

- Why is it important to identify what numbers represent different variables in a simple interest problem?
- Were there any problems in which it was difficult to figure out what numbers were the principal, rate, and time?

9. ALGEBRAIC EXPRESSIONS & IDENTITIES

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | t area / Learning Objectives Learning Outco | |
|---|--|--|
| Monomials, Binomials and Polynomials | Count the number of terms in an algebraic expression in order to classify them as monomial, binomial, trinomial or polynomial in general | |
| Addition and Subtraction of Algebraic Expressions | Identify like and unlike terms in algebraic expressions in order to add or subtract the given algebraic expressions | |
| Multiplying a Manamial by | Use rules of exponents and powers in order to multiply a monomial by a monomial | |
| Multiplying a Monomial by a Monomial | Extend the multiplication of monomial by a monomial in order to obtain the product of any number of monomials | Apply distributive property in |
| Multiplying a Monomial by | Use distributive property of multiplication over addition and subtraction in order to obtain the product of a monomial and a binomial | order to multiply two algebraic expressions |
| a Polynomial | Use distributive property of multiplication over addition and subtraction in order to obtain the product of a monomial and a trinomial | |
| | Simplify the algebraic expressions in order to find the value of expression for the given value of the variable | |
| by a Polynomial | obtain the product of two binomials | |
| | Use distributive law of multiplication in order to obtain the product of a binomial and a trinomial | |
| What is an Identity? | Define and compare equation and identity in order to classify a given question into either of the two | |
| Standard Identities | Use multiplication of binomials in order to explore and verify the standard identities for squares of binomials | Use various algebraic identities in order to solve problems of daily |
| | Use identities in order to simplify the given algebraic expressions | life |
| | Use identities in order to find the product of the given numbers | |

Test items



LOB: Count the number of terms in an algebraic expression in order to classify them as monomial, binomial, trinomial or polynomial in general

I. Which of these expressions is an example of a binomial?

Option I: $4xy^2$ **Option 2:** $4 \times y^2$ **Option 3:** $4(x + 2y^2)$ **Option 4:** $7x - 8y^2 - 5$ **Correct Answer:** Option 3

2. If $ax^n + bx - 1$ is a binomial, which of these must be true? Option 1: n = 1 or n = 0Option 2: a = bOption 3: n = 2Option 4: a = b = -1

Correct Answer: Option 1

LOB: Identify like and unlike terms in algebraic expressions in order to add or subtract the given algebraic expressions

1. What is the sum of the expressions $4x + 3y^2$, $7xy - 4y^2$ and $6x^2 - x$? **Option 1:** $6x^2 + 3x + 7xy + y^2$ **Option 2:** $6x^2 + 3x - 7xy - y^2$ **Option 3:** $6x^2 + 3x - 7xy + y^2$ **Option 4:** $6x^2 + 3x + 7xy - y^2$ **Correct Answer:** Option 4

2. The sum of polynomial ax^m and bxⁿ is 14x⁴. Which of these is correct about the values of a, b, m and n?
Option 1:a = b = 14 and m = n = 4
Option 2: a + b = 14 and m = n = 4
Option 3:a = b = 14 and m + n = 4
Option 4:a + b = 14 and m + n = 4
Correct Answer: Option 2

LOB: Use rules of exponents and powers in order to multiply a monomial by a monomial

- 1. What is the product of expressions $-4xy^2$ and $7xy^2z^3$? **Option 1:** $28x^2y^4z^3$ **Option 2:** $28xy^2z^3$ **Option 3:** $-28xy^2z^3$ **Option 4:** $-28x^2y^4z^3$ **Correct Answer:** Option 4
- 2. The product of polynomial px^c and qx^d is 8x⁶. Which of these is correct about the values of p, q, c and d?
 Option 1: p + q = 8 and c + d = 6
 Option 2: p × q = 8 and c × d = 6
 Option 3: p × q = 8 and c + d = 6
 Option 4: p + q = 8 and c × d = 6

```
Correct Answer: Option 3
```

LOB: Extend the multiplication of monomial by a monomial in order to obtain the product of any number of monomials

```
I. The product of polynomials 4xy<sup>2</sup>, -7yz and 0.5x<sup>2</sup>yz<sup>3</sup> is kx<sup>3</sup>y<sup>4</sup>z<sup>t</sup>, where k and t re unknown constants. What are the values of k and t?
Option 1: k = 14 and t = 3
Option 2: k = -14 and t = 4
```

```
Option 3: k = 28 and t = 3
Option 4: k = -28 and t = 4
Correct Answer: Option 2
```

2. The product of polynomials $-6tu^3$, $-t^3u^j$ and $-3t^ku^k$ is $-18t^7u^8$, where j and k are unknown constants. What are the values of j and k?

Option 1: j = 2 and k = 3 **Option 2:** j = 3 and k = 2 **Option 3:** j = 5 and k = 3**Option 4:** j = 1 and k = 4

Correct Answer: Option 1

LOB: Use distributive property of multiplication over addition and subtraction in order to obtain the product of a monomial and a binomial

1. What is the product of polynomials $(t^4u - 6tu^2)$ and -3tu? **Option 1:** $3t^5u^2 + 18t^2u^3$ **Option 2:** $3t^5u^2 - 18t^2u^3$ **Option 3:** $-3t^5u^2 + 18t^2u^3$ **Option 4:** $-3t^5u^2 - 18t^2u^3$ **Correct Answer: Option 3**

2. Namrata's work to find the product of $7m^2n$ and $(-6m^3n - 3n^5)$ is shown. Step 1: $7m^2n \times (-6m^3n - 3n^5)$ Step 2: $7m^2n \times (-6m^3n) - 7m^2n \times (-3n^5)$ Step 3: $-42m^5n^2 + 21m^2n^6$ In which step did she make her first error and what is the correct step? Option 1: Step 2; $7m^2n \times (-6m^3n) + 7m^2n \times (3n^5)$ Option 2: Step 2; $7m^2n \times (-6m^3n) + 7m^2n \times (-3n^5)$ Option 3: Step 2; $7m^2n \times (6m^3n) + 7m^2n \times (-3n^5)$ Option 4: Step 3; $42m^5n^2 - 21m^2n^6$ Correct Answer: Option 2

LOB: Use distributive property of multiplication over addition and subtraction in order to obtain the product of a monomial and a trinomial

1. The product of $6x^2y$ and $xy - 4x^3y + 3xy^7$ is $6x^3y^2 + p + 18x^3y^8$, where p is a term. Which of these is equivalent to p? Option 1: $24x^5y^2$ Option 2: $-24x^5y^2$ Option 3: $24x^6y^2$ Option 4: $-24x^6y^2$ Correct Answer: Option 2

2. The product of $-4x^p y$ and $xy^2 - 3x^q y + rxy$ is $-4x^4 y^3 + 12x^8 y^2 + 20x^4 y^2$, here p, q and r are unknown constants. What are the values of p, q and r? **Option 1:** p = 3, q = 5 and r = 5

Option 2: p = 3, q = 5 and r = -5 **Option 3:** p = 3, q = 3 and r = -5 **Option 4:** p = 4, q = 3 and r = -5**Correct Answer:** Option 2

LOB: Simplify the algebraic expressions in order to find the value of expression for the given value of the variable

1. What is the value of the expression 4x(3-x) + 5x(x-2) for x = -3? **Option 1:** -15 **Option 2:** -3 **Option 3:** 3

```
Option 4: 15
Correct Answer: Option 3
```

2. The value of the expression $5x(4x - x^2) + 2x(2x^2 - 5x)$ is 0 for x = t, where t is a number. Given that $t \neq 0$, which of these can be the value of t?

```
Option 1: -10
Option 2: -4
Option 3: 4
Option 4: 10
Correct Answer: Option 4
```

LOB: Use distributive law of multiplication in order to obtain the product of two binomials

If the product of (4x + 1) and (x + 4) is ax² + bx + c, what is the value of a + b + c?
 Option 1: 22
 Option 2: 24
 Option 3: 25
 Option 4: 26
 Correct Answer: Option 3

2. The length of a rectangle is $(4j^2 + 6jk)$ meters and the breadth of the rectangle is $(7jk - 3k^2)$ meters. What is the area of the rectangle?

Option 1: $28j^3k + 18jk^3$ square meters Option 2: $28j^3k - 18jk^3$ square meters Option 3: $28j^3k + 30j^2k^2 - 18jk^3$ square meters Option 4: $28j^3k - 30j^2k^2 - 18jk^3$ square meters Correct Answer: Option 3

LOB: Use distributive law of multiplication in order to obtain the product of a binomial and a trinomial

- 1. The product of polynomial (-7x + y) and (x 3y 8xyz) is $-7x^2 + m 3y^2 + 56x^2yz + k$, where m and k are terms. Which of these is equivalent to m and k? **Option 1:** m = 22xy and $k = 8xy^2z$ **Option 2:** m = 22xy and $k = -8xy^2z$ **Option 3:** m = -22xy and $k = 8xy^2z$ **Option 4:** m = -22xy and $k = -8xy^2z$ **Correct Answer:** Option 2
- 2. The area of the base of a cuboidal box is $(16l^2 + 4b^2 + 8lb)$ square meters and the height of the box is (5l 2b) meters. What is the volume of the cuboidal box?

Option I: $80l^3 - 8l^2b - 4lb^2 - 8b^3$ cubic meters **Option 2:** $80l^3 + 8l^2b - 4lb^2 - 8b^3$ cubic meters **Option 3:** $80l^3 - 8l^2b + 4lb^2 - 8b^3$ cubic meters **Option 4:** $80l^3 + 8l^2b + 4lb^2 - 8b^3$ cubic meters **Correct Answer:** Option 4

LOB: Define and compare equation and identity in order to classify a given question into either of the two

- 1. Which of the equalities is also an identity? Equality A: $a^2 + 6a + 7 = 16$ Equality B: $a^2 + 2ab + b^2 = (a + b)^2$ Equality C: $a^2 - b^2 = (a + b)(a - b)$ Option 1: Only equality B Option 2: Only equality C Option 3: Both equalities B and C Option 4: Equalities A, B and C Correct Answer: Option 3
- 2. Consider the equality shown below: Equality: $a^2 - b^2 = (a + b)(a - b)$ Which of these statements is true?

Option 1: The equality holds for all values of a and b. Option 2: The equality holds for any value of a and only b = 0. Option 3: The equality holds only for positive values of a and b. Option 4: The equality holds for only positive values of a and negative value of b. Correct Answer: Option 1

LOB: Use multiplication of binomials in order to explore and verify the standard identities for squares of binomials

1. Which option shows the correct steps to prove the identity of $(a - b)^2$? **Option 1:** $(a - b)(a - b) = a^2 - ab + ba - b^2 = a^2 - b^2$ **Option 2:** $(a - b)(a - b) = a^2 - ab + ba + b^2 = a^2 + b^2$ **Option 3:** $(a - b)(a - b) = a^2 - ab - ba + b^2 = a^2 - 2ab + b^2$ **Option 4:** $(a - b)(a - b) = a^2 - ab - ba - b^2 = a^2 - 2ab - b^2$ **Correct Answer:** Option 3

2. Trisha's work to verify the identity (a + b)(a - b) is shown below:
Step 1: a(a - b) + b(a - b)
Step 2: a² - ab + ba + b²
Step 3: a² - ab + ab + b²
Step 4: a² + b²
Given that she made an error, in which step did she make her first error?
Option 1: Step 1
Option 2: Step 2
Option 3: Step 3
Option 4: Step 4
Correct Answer: Option 2

LOB: Use identities in order to simplify the given algebraic expressions

1. Which of these is equivalent to $(3x - 4y)^2$? Option 1: $3x^2 - 4y^2$ Option 2: $9x^2 - 16y^2$ Option 3: $9x^2 - 24xy - 16y^2$ Option 4: $9x^2 - 24xy + 16y^2$ Correct Answer: Option 4

2. The expression $(9x^2 - 25)^2 - (9x^2 + 25)^2$ is equivalent to $-(t^2)$ where t is a monomial. Which of these is equivalent to t?

```
Option 1: 15x

Option 2: 30x

Option 3: 300x

Option 4: 900x

Correct Answer: Option 2
```

LOB: Use identities in order to find the product of the given numbers

```
    To find the value of 1003 × 997, a student rewrite it as 1000<sup>2</sup> - k. What is the value of k?
    Option 1: 3
    Option 2: 6
    Option 3: 9
    Option 4: 81
    Correct Answer: Option 3
```

2. To find the value of 196 × 206, a student rewrite it as 200² + q × 200 - 24. What is the value of q?
Option 1: -2
Option 2: 2
Option 3: 8
Option 4: 10
Correct Answer: Option 2

Suggested Teacher Resources



Lesson Plan



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| Objective | Identify like and unlike terms in algebraic expressions in order to add or subtract the given algebraic expressions |
|--------------------|--|
| Prerequisite | Addition and subtraction of constants, basic understanding of variables |
| Vocabulary words | Algebraic expressions |
| Materials required | Algebraic tiles or coloured chalks |
| Procedure | Teacher will start with an opening activity: |
| | Setup: Use a colour like green to represent + algebraic variable and red for negative variables as follows. |
| | X^2 $-X^2$ X X 1 1 |
| | Rules: |
| | Zero pairs |
| | Say: We know $x^2-x^2 = 0$ which can be represented as $x^2+(-x^2) = 0$. Similarly, $x + (-x) = 0$ and $1 + (-1) = 0$. After representing the numbers using tiles as shown above figure we will get. |
| | $\frac{1}{x^2} + \frac{1}{x^2} = 0$ |
| | x + -x = 0 |
| | 1 + -1 = 0 |
| | . 80 |





Example 3: What equation does



represent?

Ans: x²-2x-1

Addition:

Now the teacher will demonstrate addition of two algebraic expressions

 $(5x^2 - 4x + 5)$ and (9x - 10)

1. $5x^2 - 4x + 5$ is represented as follows







| | X^{2} X^{2} X^{2} X^{2} X^{2} X |
|----------------------|--|
| | X-X X-X |
| | 4. Remove the required expression which is $3x^2 - 6x + 4$. |
| | Follow Up Discussion: Let students work in pairs and ask them to give 5 practice questions to each other. |
| Additional resources | Exemplar sheets, support material |



Objective: Students will be able to express growth of the square pattern in algebraic expressions

Material required: Coloured chalks to represent different patterns

Setup:

- There are 4 growth patterns A, B, C and D are shown below with each pattern having 4 cases.
- Students will explore what other cases such as 10th case, 100th case, 0 case or nth case will look like.
- Students will make an algebraic expression that will represent the number of squares in the pattern at any given case.



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Steps:

- Teacher will divide the students into groups of 5.
- Show pattern B as shown above to each group. Give them 15 min to discuss the following questions:
 a) How do they see the pattern growing?
 - b) How will the case 10 look like?
 - c) How many squares will case 100 have?
 - d) How many squares will case 0 have?
 - e) How many squares will case n have?
- After discussion the teacher will ask the students to fill the following table.

Here is an example of for case B

| Make use of table using numbers | | Note down your misconceptions/ important notes |
|---------------------------------|-----------------------------|---|
| | | |
| Case | Number of blocks | |
| 1 | 1 | |
| 2 | 2 | |
| 3 | 3 | |
| 4 | 4 | |
| 5 | 5 | |
| • | | |
| | | |
| | | |
| Ν | n | |
| Draw and describe the way | y the pattern is increasing | Describe your pattern using an algebraic expression |
| or decreasing. | | that shows the number of blocks in any case number |
| | | |
| | | Algebraic expression – x |
| | | Where x is number of blocks |

• Teacher will ask the students to do the same for A, C and D.

Additional task: Ask students to create their own patterns and exchange them with their partners to solve.

Teacher's notes:

- I. How are students reasoning about extending the pattern when the answers are less clear?
- 2. Are students seeing the relationship between case number and number of squares?
- 3. How are students moving from written descriptions of patterns to algebraic expressions?

References:

- I. https://mathbits.com/MathBits/AlgebraTiles/AlgebraTiles/AlgebraTiles.html
- 2. https://www.youcubed.org/resource/k-8-curriculum

10. VISUALIZING SOLID SHAPES

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|----------------------------|--|--|
| | Compare 2D shapes and 3D shapes in order to classify a given shape into either | |
| Views of 3D- | Identify different shapes in nested objects in order to match the object with its shape | |
| Shapes | Visualize 3D objects in order to draw them from different perspectives | |
| | Discuss the given front, top and side view of an object in order to identify the object | Visualize 3-D shapes in order to represent them in a plane surface |
| | Discuss the elements in a map in order to differentiate between a map and a picture | such as sheet of paper, black board, etc. |
| Mapping Space Around Us | Read and interpret simple map in order to answer questions based on them | |
| | Choose appropriate scale and use symbols to denote landmarks in order to draw a simple map | |
| Faces, Edges and | Identify faces, edges and vertices in a given solid in order to classify it as a polyhedron or a non-polyhedron | |
| Vertices | Count vertices, edges and faces in 3D figures with flat faces in order to verify Euler's formula | Analyze patterns in order to verify Euler's relation |





LOB: Compare 2D shapes and 3D shapes in order to classify a given shape into either

I. Which of the following is NOT a 2D shape?



2. A picture frame is shown below.



Which statement is true?

Option 1: There are 2 more 3D shapes in the picture frame than 2D shapes.
Option 2: There are 2 more 2D shapes in the picture frame than 3D shapes.
Option 3: There are 3 more 3D shapes in the picture frame than 2D shapes.
Option 4: There are 3 more 2D shapes in the picture frame than 3D shapes.
Correct Answer: Option 1

LOB: Identify different shapes in nested objects in order to match the object with its shape

I. A figure is shown below.

Which of the following is true about the figure? **Option 1:** A cube is inside a circle. **Option 2:** A circle is inside a cube. **Option 3:** A square is inside a circle. **Option 4:** A circle is inside a square. **Correct Answer:** Option 4 LOB: Visualize 3D objects in order to draw them from different perspectives

I. An object is shown below.



Which of the following is the top view of the object?



Correct Answer: Option 4

2. Two objects A and B are shown below.



Which of the following statement is true?

Option I: Only the top view of objects A and B are the same.

Option 2: Only the side view of objects A and B are the same.

Option 3: Only the top and side view of objects A and B are the same.

Option 4: The top, side and front view of objects A and B are the same. Correct Answer: Option 3

LOB: Discuss the given front, top and side view of an object in order to identify the object









Correct Answer: Option I

2. Manish drew a map where he highlighted a hospital as dark grey and clinic as light grey. The distance between the hospital and the clinic is 10 km. He drew a map with a scale of 1 cm = 5 km. Which of the following maps show Manish's work?





2. Two objects are shown below.



Jasmine claims that object A is polyhedron whereas object B is not. Is her claim correct, why?

Option I: Yes, because all faces of object A are polygons and object B has only some faces as polygons.

Option 2: Yes, because all faces of object A are rectangles and object B has only some faces as rectangles.

Option 3: No, because some faces of object A are convex polygons and object B has all faces as convex polygons.

Option 4: No, because some faces of object A are rectangles and object B has all faces as rectangles.

Correct Answer: Option I

LOB: Count vertices, edges and faces in 3D figures with flat faces in order to verify Euler's formula

I. A cube is shown below.



Which of the following is true about the cube? **Option 1:** Faces: 6, Edges: 12, Vertices: 8 **Option 2:** Faces: 4, Edges: 8, Vertices: 8 **Option 3:** Faces: 6, Edges: 8, Vertices: 8 **Option 4:** Faces: 4, Edges: 12, Vertices: 8 **Correct Answer:** Option 1

2. Which of these shows the Euler's relation for a prism whose base has 5 sides?

Option 1: 6 + 6 = 10 + 2 Option 2: 6 + 8 = 10 + 4 Option 3: 10 + 7 = 15 + 2 Option 4: 10 + 9 = 15 + 4 Correct Answer: Option 3

Suggested Teacher Resources



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| Objectives Prerequisite Knowledge Material Required | Compare 2D shapes and 3D shapes in order to classify a given shape into either. Identify different shapes in nested objects in order to match the object with its shape. Visualize 3D objects in order to draw them from different perspectives. Basic knowledge of common shapes (Triangle, Square, and Rectangle etc.) Pop sticks and 3D shapes. Printed worksheets. Pen/pencil and notebooks. |
|---|--|
| Procedure | Teacher will show the following shapes to the students. She will ask them to draw these shapes in their notebooks. |





Objective: To draw objects as viewed from different positions. **Prerequisite**: knowledge of making solid shaped using unit cubes. **Material required**: Unit cubes, tapes **Procedure**:

- 1. Take some unit cubes and make the shape shown in fig. 9(a)
- 2. Now draw shapes when viewed from the front, side and top.
- 3. Repeat the activity by making other shapes. Fig, 9(b) to 9(d)



Extension: you may extend this activity for drawing different views of some more 3D objects from real life.

II. MENSURATION

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome | |
|---|---|--|--|
| Adjoint figures | Calculate area and perimeter of circle, square, rectangle, triangle in order to calculate area and perimeter of adjoint shapes | Use square grid/graph sheet in order to estimate the areas of various polygons | |
| Area of Trapezium | Breakdown a given trapezium into known figures (triangles, squares, rectangles) in order to derive the formula for the area of a trapezium | | |
| Area of a Polygon | Calculate the area of a given polygon after breaking down the polygon in multiple ways in order to compare the values and comment on it | Uses appropriate methods to find the area of a polygon | |
| Surface Area of Cube, Cuboid and Cylinder | Illustrate 2-D representation of a cuboid, cube and cylinder in order to compute the surface areas by breaking them in to areas of known figures Calculate the surface area of a cube, cuboid and cylinder to determine the cost of painting/covering their surface | | |
| Volume of Cube, Cuboid and Cylinder | Calculate the volume of a given cube, cuboid, cylinder in order to infer the quantity of any substance it can hold Modify the values of I, b, h in order to examine the effect it has on the value of the surface area/volume of a cuboid Modify the values of r, h in order to examine the | Use appropriate formulae in order to find surface area and volume of cuboidal and cylindrical object | |
| | effect it has on the value of the surface area/volume of a cylinder Calculate the volume of a given cuboid, cylinder in order to determine the time taken to fill it with a liquid at a given rate | | |



2. A park is in the shape of a trapezium, which is breakdown into 2 triangular parts and one rectangle, as shown below.



If the perpendicular distance between two parallel sides of the park is 12 m, which option correctly represents the area of the park?

Option I: $(\frac{1}{2} \times 5 \times 12) + (14 \times 12) = 198 \text{ m}^2$ **Option 2:** $2(\frac{1}{2} \times 5 \times 12) + (14 \times 12) = 228 \text{ m}^2$ **Option 3:** $(\frac{1}{2} \times 13 \times 12) + (24 \times 12) = 366 \text{ m}^2$ **Option 4:** $2(\frac{1}{2} \times 13 \times 12) + (24 \times 12) = 444 \text{ m}^2$ **Correct Answer:** Option 2

LOB: Calculate the area of a given polygon after breaking down the polygon in multiple ways in order to compare the values and comment on it

I. Consider a polygon shown.



If the length of KL and NE is the same, what is the area of the polygor Option 1: 116 cm² Option 2: 138 cm² Option 3: 144 cm² Option 4: 204 cm² Correct Answer: Option 3 **LOB:** Illustrate 2-D representation of a cuboid, cube and cylinder in order to compute the surface areas by breaking them in to areas of known figures

I. The 2-D representation of a cube is shown below.



Which expression represents the total surface area of the cube? **Option 1:** 3^2 **Option 2:** $3^2 + 3^2 + 3^2 + 3^2$ **Option 3:** $3^2 + 3^2 + 3^2 + 3^2 + 3^2 + 3^2$ **Option 4:** $3^2 + 3^2 + 3^2 + 3^2 + 3^2 + 3^2 + 3^2$ **Correct Answer:** Option 3

2. Consider the 2-D representation of 2 solids shown below.



Which solid has greater total surface area and by how much? (Use $\frac{22}{7}$ for π)

Option 1: Solid B has greater total surface area than solid A by 11 cm² Option 2: Solid A has greater total surface area than solid B by 82 cm² Option 3: Solid B has greater total surface area than solid A by 226 cm² Option 4: Solid A has greater total surface area than solid B by 324 cm² Correct Answer: Option 3

LOB: Calculate the surface area of a cube, cuboid and cylinder to determine the cost of painting/covering their surface

I. Urvashi wants to polish the exterior of a cuboidal wooden jewellery box as shown.



If the cost to polish is `0.75 per square inch, what is the cost to polish the jewellery box? Option 1: `300 Option 2: `400 Option 3: `600 Option 4: `800 Correct Answer: Option 3 2. Divya makes two cylindrical models, A and B, of diameter 21 cm each for an art project. The height of model B is 2 more than the height of model B. She wants to paint the curved surface of the models. She paints a total of 396 square metres of model A.

If the cost to paint is 0.25/sq. m, what is the total cost to paint both the models? (Use $\frac{22}{\pi}$ for π)

Option 1: `132 Option 2: `231 Option 3: `264 Option 4: `363 Correct Answer: Option 2

LOB: Calculate the volume of a given cube, cuboid, cylinder in order to infer the quantity of any substance it can hold

1. A cylindrical tank, of radius 0.35 m and height 0.70 m, is filled with water. How many cubic metres of water, to the nearest hundredth, is contained in the tank? (Use $\frac{22}{7}$ for π)

```
Option 1: 0.27
Option 2: 1.54
Option 3: 1.93
Option 4: 2.31
Correct Answer: Option 1
```

2. The areas of the three adjacent faces of a cuboidal container are 60,000 cm², 80,000 cm² and 1,20,000 cm². If the container is filled with liquid and the cuboid has whole number side lengths, how much litres of liquid is contained in the container?

```
Option 1: 9,000
Option 2: 24,000
Option 3: 26,000
Option 4: 52,000
Correct Answer: Option 2
```

LOB: Modify the values of I, b, h in order to examine the effect it has on the value of the surface area/volume of a cuboid

1. If the length of a cuboid is reduced to its half and breadth become four times, how does the volume of the cuboid change?

Option 1: It will become 2 times Option 2: It will remain the same Option 3: It will reduce to half Option 4: It will become four times Correct Answer: Option 1

2. A cuboid is x metres long, y metres wide and z metres deep. If the length becomes one-fourth and breadth become three times, which expression represents the change in the lateral surface area of the cuboid?

```
Option I: (\frac{x}{2} + 6y)z

Option 2: (\frac{3x}{2} - 4y)z

Option 3: (\frac{3xy}{2} + 6yz + \frac{xz}{2})

Option 4: (\frac{xy}{2} - yz + \frac{3}{2}xz)
```

Correct Answer: Option 2

LOB: Modify the values of I, b, h in order to examine the effect it has on the value of the surface area/volume of a cuboid

1. If the height of a cylinder triples and its radius becomes one-third, how does the lateral surface area of the cylinder change?

Option I: It becomes one-third **Option 2:** It becomes triple

Option 3: It remains the same Option 4: It will increase by 3 Correct Answer: Option 3

2. The radius and height of a cylinder is 6 cm and 9 cm respectively. If the radius becomes half and the height increases by 3 cm, which of these describes the new volume of the cylinder?

Option I: The new volume will be half the original volume.

Option 2: The new volume will be twice the original volume.

Option 3: The new volume will be thrice the original volume.

Option 4: The new volume will be one-third the original volume.

Correct Answer: Option 4

LOB: Calculate the volume of a given cuboid, cylinder in order to determine the time taken to fill it with a liquid at a given rate

I. Akriti is filling oil into a cylindrical container of radius 50 cm and height 105 cm, at the rate of 5 litres per minute. How many minutes will she take to fill the container completely? (Use $\frac{22}{\pi}$ for π)

Option 1: 41.25 Option 2: 45 Option 3: 125 Option 4: 165 Correct Answer: Option 4

2. A cuboidal tank of dimensions 3m, 4m, and 5m has 3 litres of water. Two pumps, P and Q, are used to fill the remaining volume of the tank completely with water. Pump P fills the tank at a rate of 1000 litres per 20 minutes and pump Q fills the tank at a rate of 240 litres per 3 minutes. First, the pump P fills 9 m³ of the tank and then, pump Q fills the remaining volume. In how many hours will both the pumps completely fill the tank?

Option 1: 2.5 hours Option 2: 3 hours Option 3: 5.5 hours Option 4: 6.125 hours Correct Answer: Option 4



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| Draw the pattern shown on a squared paper and cut it out [Fig (i)]. (You know that this pattern is a net of a cube. Fold it along the lines [Fig (ii)] and tape the edges to form a cube |
|--|
| |
| Teacher will discuss the following points with students: |
| a) What is the length, width and height of the cube?b) Observe that all the faces of a cube are square in shape. This makes |
| length, height and width of a cube equal (Fig (i)). |
| c) Write the area of each of the faces. Are they equal? d) Write the total surface area of this suba |
| e) If each side of the cube is I, what will be the area of each face? (Fig |
| (ii)). Can we say that the total surface area of a cube of side I is 612? |
| 6. How to make the net of a cylinder: Take a cylindrical can or box and trace the base of the can on graph paper and cut it [Fig (i)]. |
| • Take another graph paper in such a way that its width is equal to the height |
| Of the can. Wrap the strip around the can such that it just fits around the can (remove) |
| the excess paper) [Fig (ii)]. |
| Tape the pieces [Fig (iii)] together to form a cylinder [Fig(iv)]. What is the shape of the paper that goes around the cap? Of course, it is |
| rectangular in shape. |
| • When the parts of this cylinder are taped together, the length of the |
| rectangular strip is equal to the circumference of the circle. • Record the radius (r) of the circular base length (l) and width (b) of the |
| rectangular strip. Is $2\pi r = \text{length of the strip.}$ |
| Check if the area of the rectangular strip is 2πrh. |
| • Count how many square units of the squared paper are used to form the cylinder. Check if this count is approximately equal to $2\pi r$ (r + h). |
| me andre of me babet mue Poes mount me emit |
| |
| • We can deduce the relation $2\pi r$ (r + h) as the surface area of a cylinder in |
| another way. Imagine cutting up a cylinder as shown below. |
| - |
| 2nr |
| |
| - <u> </u> |
| |
| 7. Teacher will ask students to fill in the following table |
| 105 |

| Shape | Lateral Surface area | Total Surface area |
|----------------------------|----------------------|--------------------|
| Cube Cuboid Cylinder | | |



Prerequisite: Total surface area and lateral surface area of cube and cuboid. **Materials required:** Measuring tape or scale **Introduction:**

- 1. Teacher will introduce the activity to students by explaining a cube is made of many small unit cubes and will then show the following cases to students:
- a) Imagine that we paint a 4 by 4 by 4 cube blue on every side as shown here.



Answer the following questions:

- How many of the small cubes have 3 blue faces?
- How many have 2 blue faces?
- How many have I blue face?
- How many have not been painted at all?
- How many faces would be painted in a cube of any size?
- Answer the above questions for case 2 and case 3?

2. Teacher will give a rough estimation of the dimensions of the classroom to the students. Students in the groups of 5 can be tasked to find how much it will cost to paint the walls of their classroom at the rate of Rupees 7.50 per m².

Reference:

- I. <u>http://ncert.nic.in/textbook/textbook.htm?hemh1=11-16</u>
- 2. <u>http://www.ncert.nic.in/departments/nie/niew/school_kits/upper_prm_level/pdf/kit_manual_UP_math.pdf</u>
- 3. <u>https://bhi61nm2cr3mkdgk1dtaov18-wpengine.netdna-ssl.com/wp-content/uploads/2017/03/Painting-Youcubed-2016.pdf</u>

12. EXPONENTS AND POWERS

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|---|---|---|
| Powers with Negative Exponents | Simplify powers with negative exponents in order to calculate the multiplicative inverse of a number | |
| Laws of Exponents | Give examples in order to show that is valid for all integer exponents. Apply the first law of exponents () and principles of negative exponents in order to derive the rest of the laws of exponents | Apply rules of exponents in order to solve problems with integral |
| | Apply laws of exponents in order to simplify a given expression | exponents |
| Use of Exponents to Express Small Numbers in Standard Form | Express very large and very small numbers in the standard form in order to compare and estimate quantities | |


```
For which of these expressions can we use the formula, (z^a)^b = z^{ab}?

Option 1: Only (10^2)^4, as it holds true only for positive integer exponents.

Option 2: Only (10^{-3})^{-9}, as it holds true only for negative integer exponents.

Option 3: All (10^5)^{-2}, (10^2)^4 and (10^{-3})^{-9}, as it holds true for all integer exponents.

Option 4: Only (10^5)^{-2} and (10^{-3})^{-9}, as it holds true only for negative integer exponents.

Correct Answer: Option 3
```

LOB: Apply the first law of exponents $[a^m X a^n = a^m+n]$ and principles of negative exponents in order to derive the rest of the laws of exponents

I. Which of the following is equivalent to $5^8 \times 5^{-3}$? Option 1: $5^{(8+3)}$ Option 2: $5^{(8-3)}$ Option 3: $5^{[8\times(-3)]}$ Option 4: $5^{(-8-3)}$ Correct Answer: Option 2

```
2. If (p^3 \times p^{-2}) \times (q^5 \times q^{-3}) = 50, then what are the values of p and q?

Option 1: p = 2 and q = 5

Option 4: p = 4 and q = 5

Option 2: p = 2 and q = 25

Option 3: p = 4 and q = 25

Correct Answer: Option 1
```

 $\ensuremath{\textbf{LOB:}}$ Apply laws of exponents in order to simplify a given expression

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1. Which of these is the simplified form of the expression $[(-7)^5 \times (-7)^2] \div (-7)^4$? Option 1: $(-7)^3$ Option 2: $(-7)^6$ Option 3: $(-7)^7$ Option 4: $(-7)^{11}$ Correct Answer: Option 1 2. What is the simplified form of the expression $\left(\frac{p^r}{p^s}\right)^{r+s} \left(\frac{p^s}{p^t}\right)^{s+t} \left(\frac{p^t}{p^r}\right)^{r+t}$? Option 1: 0 Option 2: 1 Option 3: $p^{2(r^2+s^2+t^2+rs+st+rt)}$ Option 4: $p^{2(r^2-s^2-t^2+rs+st+rt)}$

Correct Answer: Option 2

LOB: Express very large and very small numbers in the standard form in order to compare and estimate quantities

1. The population of a bacteria in dish A is 3.2×10^8 and in dish B is 0.7×10^7 . What is the total population of bacteria in both the dishes?

Option I: 3.9×10^{8} Option 2: 3.27×10^{7} Option 3: 3.27×10^{8} Option 4: 1.02×10^{7} Correct Answer: Option 3

2. Which option correctly describes the set of all possible values of j that make the given comparison true? $3.08 \times 10^{-4} > j \times 10^{-3}$

Option 1: All numbers less than 3.08 Option 2: All numbers greater than 3.08 Option 3: All numbers less than 0.308 Option 4: All numbers greater than 0.308 Correct Answer: Option 3 www.cbseteachers.in

Suggested Teacher Resources



Lesson Plan



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| Objective | Students will be able to simplify powers with negative exponents in order to calculate the multiplicative inverse of a number | | |
|--------------------|--|---|----------------------------------|
| Prerequisite | Multiplication, exponential representation | | |
| Vocabulary words | Exponents | | |
| Materials required | Worksheet | | |
| Procedure | Start the class with an activity. Teacher will group the students in pairs. Students have to represent 32 as power of 2 using factors. | | |
| | Answer: $2^3 - 2^{+}2^{+}2^{+}2^{+}2^{+}2^{+}2^{+}2^{+}$ | | |
| | Then students will represent 2-1 using the same steps they have been doing till now which is divided by 2. | | |
| | Exponent | Factors | Value |
| | 2 ⁵ 2 ⁴ 2 ³ 2 ² 2 ¹ 2 ⁰ 2 ⁻¹ 2 ⁻² Students will be asked to find the Teacher will give following wor The following worksheet will be | 2*2*2*2*2 2*2*22 2*2*2 2*2 2 2 2 2 2 2 | 32 16 8 4 2 1 |

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Objectives: Students will be able to simplify exponential numbers Material Required: Chart Papers

Procedure:

I. The Teacher will divide the students in groups of 4.

2. Each group will cut a circle as shown from the cut-outs. In groups of 4 they write the questions on the top, solve those questions and write the answers under the leaf of the cut-out.





3. Each group will exchange their exponents circles and solve the questions and check the answers written underneath.

4. Once the time is over, answers will be discussed in the large group

Reference:

- I. <u>https://www.teacherspayteachers.com/Product/Evaluating-Exponential-Expressions-Maze-1757743</u>
- 2. <u>https://s3.amazonaws.com/migleadmagnets/Properties+of+Exponents+Chart.pdf</u>

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13. DIRECT & INVERSE PROPORTIONS

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|--|--|--|
| Direct proportion and Inverse proportion | Observe the relationship between the given two quantities in order to solve for the constant of proportionality Examine situations in order to decide whether two quantities are proportional to each other or not Complete a given table showing two proportional quantities in order to answer questions based on them Convert the given statement on relationship (directly or inversely proportional) between two quantities into a table in order to identify the missing quantity and solve for its value Observe the table in order to determine which pair of variables are inversely proportional Create their own scale by creating the best proportionality constant in order to draw a given figure with large dimensions | Solve problems based on direct or inverse proportions in order to establish how one quantity depends on other |

Test items



LOB: Observe the relationship between the given two quantities in order to solve for the constant of proportionality

1. The quantities A and B are in direct proportion. The table below shows the values of A and the corresponding values of B.

| Α | 8 | 26 | | |
|--|----|----|--|--|
| В | 20 | 65 | | |
| What is the constant of proportionality? | | | | |

Option I: $\frac{8}{65}$ Option 2: $\frac{4}{13}$ Option 3: $\frac{2}{5}$ Option 4: $\frac{10}{13}$ Correct Answer: Option 3

2. The quantities X and Y are in direct proportion. The table below gives the values of X and Y, where m is an unknown.

| X | 6 | 9 |
|---|------------|---------|
| Y | 7 <i>m</i> | 10m + 1 |
| | | |

Which of these is the constant of proportionality?

```
Option I: \frac{1}{11}
Option 2: \frac{1}{3}
Option 3: \frac{3}{7}
Option 4: \frac{2}{3}
Correct Answer: Option 3
```

LOB: Examine situations in order to decide whether two quantities are proportional to each other or not

I. Which of the following situations is an example of direct proportion?

Option I: The perimeter *p* of a square and its side length *a*.

Option 2: The length *l* and the width *w* of a rectangle, given the area remain constant.

Option 3: The number of units of a product that can be purchased given a fixed amount of money, and the unit price of the product.

Option 4: The number of rows *m* and the number of columns *n* in which a fixed number of marbles can be arranged.

Correct Answer: Option I

2. Amrita is conducting an experiment to determine how the weight of a metal changes with its volume. Based on the data she collected from the experiment, she made the following observations.

Observation I: As the volume of the metal increases, the weight of the metal also increases.

Observation 2: The weight of the metal per cubic centimetre remains constant.

Which observation(s) is/are sufficient to conclude that the weight and the volume of the metal are in direct proportion?

Option 1: Only observation 1 is sufficient. **Option 2:** Only observation 2 is sufficient.

Option 3: Both observations are required.

Option 4: Neither observation is sufficient.

Correct Answer: Option 3

LOB: Complete a given table showing two proportional quantities in order to answer questions based on them

I. The table below shows the price and quantity of product A.

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| Price (in ₹) | 17 | 51 |
|------------------|----|----|
| Quantity (in kg) | а | b |

Which of these can be the values of a and b?

Option I: a = 6 and b = 18

Option 2: a = 18 and b = 6**Option 3:** a = 16 and b = 50

Option 4: a = 3 and b = 289

Correct Answer: Option 1

2. The table below shows the number of units of a product that can be bought for a given amount.

| Number of units | 8 |
|-----------------|----|
| Amount (in ₹) | 24 |

Given that the unit cost is same, if the number of units bought is increased by 2p, what will be the change in the total cost?

Option 1: the total cost will decrease by 6p **Option 2:** the total cost will increase by p **Option 3:** the total cost will increase by 6p **Option 4:** the total cost will decrease by p

Correct Answer: Option 3

LOB: Convert the given statement on relationship (directly or inversely proportional) between two quantities into a table in order to identify the missing quantity and solve for its value

1. If 30 cupcakes are prepared using 500 grams of flour, how many cupcakes can be prepared by using 750 grams of flour assuming each cupcake is equal in size?

Option 1: 15 Option 2: 25 Option 3: 36 Option 4: 45 Correct Answer: Option 4

2. A dish is prepared using some quantity of wheat flour and semolina as shown in the table.

| Wheat flour | 300 grams |
|-------------|-----------|
| Semolina | 100 grams |

How many grams of semolina are needed to prepare the same dish if the quantity of wheat flour is increased by 50%?

Option 1: 50 grams Option 2: 100 grams Option 3: 150 grams Option 4: 250 grams Correct Answer: Option 3

LOB: Observe the table in order to determine which pair of variables are inversely proportional

I. In which of these tables X and Y are in inverse proportion?

| <u>Opt</u> | ion | l: |
|----------------------|------------------------------|----------------------------|
| Х | 15 | 3 |
| Y | 20 | 4 |
| Opt | ion | 2: |
| Х | 15 | 30 |
| Υ | 20 | 10 |
| | - | |
| Opt | ion | 3: |
| Opt X | ion 15 | 3: 20 |
| Opt X Y | ion 15 30 | 3: 20 10 |
| Opt X Y Opt | ion 15 30 | 3: 20 10 4: |
| Opt X Y Opt | ion 15 30 ion 15 | 3: 20 10 4: 20 |

Correct Answer: Option 2

2. Kaya and Navya have the same number of marbles. Kaya arranges the marbles in a rectangular array. The table below shows the number of rows and columns of the array.

| Number of rows | 15 |
|-------------------|----|
| Number of columns | 20 |
| | |

How many marbles are there in a column, if Navya arranged all the marbles in 5 more columns than Kaya? **Option 1:** 10

Option 2: 12 Option 3: 20 Option 4: 30 Correct Answer: Option 2

LOB: Create their own scale by creating the best proportionality constant in order to draw a given figure with large dimensions

1. To draw a model of a residential society, Jaya used a scale factor of 1:300. If the height of the building in model is 12 cm, which of these can be the actual height of the building?

Option 1: 20 m Option 2: 25 m Option 3: 30 m Option 4: 36 m Correct Answer: Option 4

2. The floor plan drawing of a square and a rectangular room is drawn using the same scale. The plan shows the area of the floor of the rectangular room as 12 cm² for the actual area of 24 m². What is the area of the floor of the square room in the plan if the actual side of the floor of the square room is 6 m?

Option 1: 10 cm² Option 2: 18 cm² Option 3: 20 cm² Option 4: 25 cm² Correct Answer: Option 2 www.cbseteachers.in

Suggested Teacher Resources



Lesson Plan



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| Prerequisite Knowledge Basic mathematical operations. Material Required • Chalk and blackboard. • Pen/Pencil and notebook. • Empty Juice box. • Pener clien to write questions | Objectives | Students will be able to examine quantities in order to decide whether two quantities are proportional to each other or not | |
|---|---------------------------|--|--|
| Chalk and blackboard. Pen/Pencil and notebook. Empty Juice box. | Prerequisite Knowledge | Basic mathematical operations. | |
| Faper sups to write questions. | Material Required | Chalk and blackboard. Pen/Pencil and notebook. Empty Juice box. Paper slips to write questions. | |
| Procedure I. Teacher will start the class by displaying a packet of juice and will ask a student to come and read its nutritional value. 2. All the students will write the information in their notebooks. For example: Apple juice 440ml, each 440ml provides: i) Carbohydrate 6.6g, iii) Carbohydrate 6.6g, iii) Carbohydrate 6.6g, iii) Carbohydrate 6.6g, iiii Paccher will ask the following questions to students: If 440 ml of juice provides 226 calories how many calories 100ml of juice will provide: How many grams of Carbohydrates would there be in 100 ml of juice? How many calories, grams carbohydrates and Vitamin C would be there in 2 litres of the juice? Now the teacher will ask students to analyse are these direct or inverse proportion questions, can they show the working? If they are unable, show working on the board Solution: 440 ml of juice contains calories = 226 /440 100 ml or juice contains carbohydrates=6.6g I ml of juice contains carbohydrates=6.6f440 100 ml of juice contains vitamin c= 0.02/440 100 ml of juice contains vitamin c= 0.02/440 100 ml of juice contains calories = 226/440 200 ml of juice contains calories = 226/440 200 ml of juice contains vitamin c= 0.02/440 200 ml of juice contains vitamin c= 0.02/440 200 ml of juice contains vitamin c= 0.02/440 200 ml of juice contains calories = 226/440 21 ml of juice contains calories = 226/440 2200 = 1027 Cal 1 ml of juice contains calories = 226/440 × | Procedure | 1. Teacher will start the class by displaying a packet of juice and will ask a student to come and read its nutritional value. 2. All the students will write the information in their notebooks. For example: Apple juice 440ml, each 440ml provides: i) Energy 226 calories, ii) Carbohydrate 6.6g, iii) Vitamin c 20 mg 3. Teacher will ask the following questions to students: If 440 ml of juice provides 226 calories how many calories 100ml of juice will provide? How many grams of Carbohydrates would there be in 100 ml of juice? How many grams of Vitamin C would be there in 100 ml of juice? How many calories, grams carbohydrates and Vitamin C would be there in 2 litres of the juice? All whe teacher will ask students to analyse are these direct or inverse proportion questions, can they show the working? If they are unable, show working on the board. Solution: 440 ml of juice contains calories = 226 I ml of juice contains calories = 226 /440 100 ml contain = 226 / 440 × 100 = 56.5 Cal 440 ml of juice contains carbohydrates=6.6g I ml of juice contains carbohydrates=6.6/440 100 ml of juice contains carbohydrates=6.6/440 100 ml of juice contains Vitamin c= 0.02/440 100 ml of juice contains vitamin c= 0.02/440 × 100 = 1.5g 440 ml of juice contains vitamin c= 0.02/440 100 ml of juice contains calories = 226/440 2 L of juice contains calorie | |

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| | 2L of juice contains Vitamin c= 0.02/440 x 2000= 0.09g 5. Teacher will then ask students to mention various examples of direct and inverse quantities from their immediate environment. 6. Follow up Discussion: Teacher will ask the students to bring packets of different products and compare their nutritional value/quantities of the ingredients in order to understand direct and inverse ratios. |
|-----------|--|
| Reference | https://aminghori.blogspot.com/2017/03/lesson-plan-of-direct-and-inverse.html |
| | |

Objective: To develop intuitive understanding of proportion through enlargement. Materials: Square dot paper

Activity

Time Required: 30 minutes

Procedure:

- I. Teacher will make pairs of students and will give a square dot paper to each pair.
- 2. Give a drawing of a letter of the alphabet or a numeral, as shown in the figure.



- 3. She will ask the students to double it. Were they able to do it correctly?
- 4. Teacher will evaluate the student's drawing basis on these questions:
 - Did their drawing seem right to them?
 - What kind of errors did they make?
 - What could have caused the errors?
- 5. Then she will ask them to triple it. Did they find any difficulty?

Extension of the activity:

Teacher can then extend the concept of proportion or scaling up/down in terms of ratios by using various examples.

Source: At Right Angles, Azim Premji University, July 2019

14. FACTORIZATION

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|----------------------------|---|------------------|
| Factors of algebraic | Express each term as a product of irreducible factors in order | |
| expressions | to find the common factors of the given terms | |
| Method of common | Use the method of common factors in order to factorize the | |
| factors | given algebraic expression | |
| Factorisation by | Regroup the terms in order to factorize the given algebraic | |
| regrouping terms | expressions | |
| Factorisation using | Apply the standard algebraic identities in order to factorize the | |
| identities | given algebraic expressions (for perfect squares) | |
| | Factorize algebraic expressions in the form in order to express | |
| Factors of the form | it as a product of its irreducible factors of the form | |
| | Use the common factor method in order to divide a monomial | - |
| | by a monomial | |
| | Use the common factor method in order to divide a | |
| Division of Algebraic | polynomial by a monomial | |
| Expressions | Divide each term in the numerator by the denominator in | |
| | order to divide a polynomial by a monomial | |
| | Use the common factor method in order to divide a | |
| | polynomial by a polynomial | |
| Find the Funen | Check the given mathematical statements in order to find and | |
| Find the Error | give reasons for the possible errors in them | |



LOB: Apply the standard algebraic identities in order to factorize the given algebraic expressions (for perfect squares)

I. Which of the following is equivalent to $81k^2 - 64$? Option I: (9k + 4)(9k - 4)Option 2: (9 + 4k)(9 - 4k)Option 3: (9 + 8k)(9 - 8k)Option 4: (9k + 8)(9k - 8)Correct Answer: Option 4

2. What is the factorized form of the expression $9x^2 + 14y - 1 - 49y^2$? Option I: (3x + 7y - 1)(3x - 7y + 1)Option 2: (3x + 7y + 1)(3x - 7y - 1)Option 3: (7y - 1 - 3x)(1 - 7y + 3x)Option 4: (7y - 1 + 3x)(1 - 7y - 3x)Correct Answer: Option I

LOB: Factorize algebraic expressions in the form $x^2 + px + q$ in order to express it as a product of its irreducible factors of the form (x + a)(x + b)

- 1. What are the factors of $k^2 + 4k 32$? **Option 1:** (k + 4) and (k - 8) **Option 2:** (k - 4) and (k + 8) **Option 3:** (k + 4) and (k + 8) **Option 4:** (k - 4) and (k - 8)**Correct Answer:** Option 2
- 2. If (x + a) and (x + b) are factors of the expression $x^2 + x 56$, where a > b, then what is the factorized form of the expression $ax^2 + ax + ab$?

Option 1: 8(x + 4)(x - 3)Option 2: 8(x - 4)(x + 3)Option 3: 4(x + 4)(x - 3)Option 4: 4(x - 4)(x + 3)Correct Answer: Option 1

LOB: Use the common factor method in order to divide a monomial by a monomial

```
1. Which of these is equivalent to 6m^4 \div 2m?

Option 1: 3 \times m

Option 2: 3 \times m \times m

Option 3: 3 \times m \times m \times m

Option 4: 3 \times m \times m \times m \times m

Correct Answer: Option 3
```

```
2. If A = (80p^2q \div 5p) \div 2q and B = (100p^2q^2 \div 10q^2) \div 2p, what is the value of A \div B?

Option 1: \frac{5}{4}

Option 2: \frac{4}{5}

Option 3: \frac{5}{8}

Option 4: \frac{8}{5}

Correct Answer: Option 4
```

LOB: Use the common factor method in order to divide a polynomial by a monomial

```
1. Which of these is equivalent to (14a - 6a^3 + 2a^5) \div 2a?

Option 1:(7 - 3a^2 + a^3)

Option 2: (7 - 6a^2 + 2a^3)
```

Option 3: $(7 + 3a^2 + a^3)$ **Option 4:** $(7 + 6a^2 + 2a^3)$ **Correct Answer:** Option I

2. Which of the following expressions when divided by $9mn^2$ does not give a polynomial? Option 1: $3(3m^2n + 18m^2n^2 - 60mn^4)$ Option 2: $2(45m^4n^2 - 9mn^2 - 36mn^3)$ Option 3: $3(21m^3n^2 + 15m^2n^5 - 6mn^2)$ Option 4: $2(56m^4n^3 - 18mn^3 + 54mn^2)$ Correct Answer: Option 1

LOB: Divide each term in the numerator by the denominator in order to divide a polynomial by a monomial

1. Which of these is equivalent to $(18h^3 - 9h^2 + 6h) \div 3h$? **Option I:** $\frac{3h(6h^2)}{3h} - \frac{3h(3h)}{3h} + \frac{3h(2)}{3h}$ **Option 2:** $\frac{3h(3h^2)}{3h} - \frac{3h(3h)}{3h} - \frac{3h(2)}{3h}$ **Option 3:** $\frac{3h(6h^2)}{3h} + \frac{3h(3h)}{3h} + \frac{3h(2)}{3h}$ **Option 4:** $\frac{3h(3h^2)}{3h} - \frac{3h(h)}{3h} + \frac{3h(2)}{3h}$ **Correct Answer:** Option I

2. Which of these is obtained by dividing
$$(36abc + 24a^2b^2c - (18a^2b^3c + 30a^2bc^2))$$
 by $3abc$?
Option I: $-6ab^2 - 10ac + 8c + 12$
Option 2: $6ab^2 - 10ac + 8c + 12$
Option I: $-6ab^2 - 10ac + 8c - 12$
Option 2: $6ab^2 - 10ac + 8c - 12$
Option 2: $6ab^2 - 10ac + 8c - 12$
Correct Answer: Option I

LOB: Use the common factor method in order to divide a polynomial by a polynomial

1. What is the quotient obtained when $(18r^2 - 32d^2)$ is divided by (3r + 4d)? Option 1: $2 \times (3r - 4d)$ Option 2: $2 \times (3r + 4d)$ Option 3: $4 \times (3r - 4d)$ Option 4: $4 \times (3r + 4d)$ Correct Answer: Option 1

2. An expression is shown below: $22(x^4 - x^3 - 20x^2)$ Vinod claims that when the expression is divided by $11x^2(x + 4)$ we get 2(x - 5). Varun claims that when the expression is divided by 11x(x + 5) we get 2x(x + 4). Who is/are correct? Option 1: Only Vinod Option 2: Only Varun Option 3: Both of them Option 4: None of them orrect Answer: Option 1

LOB: Check the given mathematical statements in order to find and give reasons for the possible errors in them

1. The steps to solve the equation 3(y + 1) + 2y = 20 are shown below. 3(y + 1) + 2y = 20Step 1: 3y + 3 + 2y = 20Step 2: 5y = 20Step 3: $y = \frac{20}{5}$ Step 4: y = 5Given that the solution is incorrect, in which step was the first mistake made?

Option I: Step | Option 2: Step 2 Option 3: Step 3 Option 4: Step 4 Correct Answer: Option 2

2. The steps to solve the equation $(x + 5)^2 - 3x = x^2 - 3$ are shown below. $(x+5)^2 - 3x = x^2 - 3$ **Step I:** $x^2 - 10x + 25 - 3x = x^2 - 3$ **Step 2:** -13x + 25 = -3

Step 3: -13x = -28

Step 4: $x = \frac{28}{13}$

Given that the solution is incorrect, in which step was the first mistake made and what is the correct solution to the equation?

Option I: Step I; –4 **Option 2:** Step 2; 4 **Option 3:** Step 3; $-\frac{22}{12}$ **Option 4:** Step 4; $-\frac{13}{13}$

Correct Answer: Option I

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Suggested Teacher Resources



Lesson Plan



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| Objectives | Use the method of common factors in order to factorize the given algebraic expression | |
|---------------------------|--|--|
| Prerequisite Knowledge | Meaning of factorization, common factors. | |
| Material Required | Chalk, duster, blackboard, Pen/Pencil and notebook | |
| Procedure | The teacher will start with a question: The area of a rectangle, in square units, is represented by $3n^2 + 3n$ for a natural number n . Find the length and width of the rectangle. The students will be given 2 minutes to list the answer(s) they find. $(3n^2 + 3n)$ square units | |
| | The following discussion should include a similar approach as below: We know that the area of a rectangle is a product of its length and breadth, i.e., $3n^2 + 3n = length \times breadth$ (of the rectangle) That means, we need to factorize the polynomial given for area to find the algebraic expressions for length and breadth. First, we need to check the Greatest Common factor (GCF) in $3n^2 + 3n$. When factoring a polynomial, we first look for a monomial that is the GCF of all the terms of the polynomial. Then, we reverse the distribution process by factoring the GCF out of each term and writing it on the outside of the parentheses. We can express $3n^2 + 3n = 3 \times n \times n + 3 \times n$, we can see that 3n is the GCF. We can take it as common and hence factorize the expression as $3n^2 + 3n = 3n(n + 1)$, where 3n and $(n + 1)$ are the two factors. Here, the width of the rectangle could be $3n$ units and the length could be $(n + 1)$ units OR the width of the rectangle could be $(n + 1)$ units and the length could be 3n units. | |
| | Note: If students try to use 1 as the common factor for two or more numbers, point out that, while 1 is indeed a factor, factoring out a 1 does not help in finding the factors of an expression. If this issue arises, it may be necessary to discuss the results when factoring out a 1. Students may opt to factor only n or 3 or even $\frac{1}{2}n$: $n(3n + 3)$ or $3(n^2 + n)$ or $\frac{1}{2}n(6n + 6)$.) There are infinite representations for the dimensions of the rectangle. | |
| | Now give students a few questions to attempt with their partners. A few have been suggested below: $30pq + 15p$ $ax^3 - bx^2 + cx$ $l^2m^2n - lm^2n^2 - l^2mn^2$ | |
| L | 123 | |

| | $\frac{18x^3y - 54x^2y + 72xy}{a^3 + a^2 + a + 1}$ |
|-----------|---|
| | The teacher will then discuss all the expressions on the board by encouraging the students to volunteer. |
| Reference | https://www.engageny.org/resource/algebra-i-module-4-topic-lesson-2 https://www.engageny.org/resource/algebra-i-module-4-topic-lesson-3 https://www.engageny.org/resource/algebra-i-module-4-topic-lesson-4 |





Instructions:

- I) The teacher will divide the class in two groups.
- 2) Group I will have to randomly choose one chit from bowl I and Group 2 will do the same from bowl 2. The teacher has to ensure that all the students have got the chit and no one is left.
- After every student has got a chit, the teacher will give I minute for them to expand/ factorize the given algebraic expression. This will be done in their notebooks. Those who got the expanded form of the expression, will need to factorize it. Those who got the factored form, will need to expand the expression.
- 4) After one minute, the teacher will instruct everyone to stop.
- 5) The teacher will then ask volunteers from each group to collect the chits from their group members and return it in the respective bowls.
- 6) The teacher will randomly choose one chit from Bowl 2, and write down the factorized form on the board. The student from Group I who has the corresponding expanded form of the factorized form on board will need to raise hand and tell the expression.
- 7) Similarly, the teacher will now randomly choose one chit from Bowl I, and write down the expanded form on the board. The student from Group 2 who has the corresponding factor form on her chit will raise a hand and tell the factor form.
- 8) Both the groups will get only 40 seconds to raise hand and answer.
- 9) The chits picked by the teacher will not go back in the bowls.
- 10) If the expression is correct then the respective Group will get 5 points, if a wrong expression is given then there will be a penalty of 3 points. If no answer is given then no points will be given.
- 11) The teacher will note the scores of both the teams on the board and will announce the winner after all the chits have been exhausted.

| S. No. | Expanded Form | Factorised form |
|--------|---------------------------|------------------------------------|
| I | $21x^2y^3 + 27x^3y^2$ | $3x^2y^2(7y+9x)$ |
| 2 | $4x^2 - 20x + 25$ | (2x-5)(2x-5) |
| 3 | 23xy - 46x + 54y - 108 | (y-2)(23x+54) |
| 4 | $6x^2y^3 + 9xy^4 + 18y^5$ | $3y^3(2x^2 + 3xy + 6y^2)$ |
| 5 | $16h^2 - 36k^2$ | (4h-6k)(4h+6k) |
| 6 | $r^4 - 16s^4$ | $(r^2 + 4s^2)(r + 2s)(r - 2s)$ |
| 7 | $x^2 - 2x + 15/16$ | (x-5/4)(x-3/4) |
| 8 | $-2x^3 - 2x^2 + 112x$ | -2x(x-7)(x+8) |
| 9 | $y^8 - 81x^4$ | $(y^4 + 9x^2)(y^2 + 3x)(y^2 - 3x)$ |
| 10 | $9x^2 - 3x - 12$ | 3(x+1)(3x-4) |

A sample of expressions has been given below:

15. INTRODUCTION TO GRAPHS

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|--|--|------------------|
| A line mesh | Draw a line graph in order to represent the given data that changes continuously over periods of time | |
| A line graph | Interpret the given line graph in order to answer the given questions | |
| | Plot a point on the graph in order to describe its coordinates | |
| Linear graph and Location of a point/coordinates | Plot the given points on the graph in order to verify if they lie on the same line or not | - |
| | Choose an appropriate scale in order to plot a graph for the given data | |
| Some applications | Construct the line graph in order to discuss the relationship between independent and dependent variable in a given mathematical situation | |





LOB: Draw a line graph in order to represent the given data that changes continuously over periods of time



I. The table below shows the run scored by a team in a 50 over match.

2. The table below shows the distance, in km, covered by two athletes on each day of last week.

| | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
|-----------|--------|---------|-----------|----------|--------|----------|
| Athlete A | 4.5 | 4.5 | 6.0 | 3.5 | 5.5 | 5.0 |
| Athlete B | 4.0 | 4.5 | 5.5 | 5.0 | 6.0 | 5.0 |

Which of these line graphs correctly represents the data?

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LOB: Interpret the given line graph in order to answer the given questions

1. The line graph below shows the number of bikes sold at a store on each day of last week.



Which of the following statements is not correct?

Option 1: The value of laptop decreases by i3000 in 2004-05. Option 2: The value of laptop decreases by i1500 in 2001-02. Option 3: The value of laptop decreases by i5800 in 2006-07. Option 4: The value of laptop decreases by i4500 in 2005-06. Correct Answer: Option 3

LOB: Plot a point on the graph in order to describe its coordinates

1. Which of the following is correct about the point R (4, 1) when plotted on a coordinate grid?

Year

Option 1: The point R lies on the x-axis.
Option 2: The point R lies on the y-axis.
Option 3: The point R lies 4 units to the right of y-axis and 1 unit up the x-axis.
Option 4: The point R lies 1 unit to the right of y-axis and 4 units up the x-axis.
Correct Answer: Option 3

2. A point T lies 6 units to the right of the y-axis. Which of these can be the coordinates of the point T?
Option 1: (0, 6)
Option 2: (6, 0)
Option 3: (3, 3)

```
Option 4: (12, 12)
Correct Answer: Option 2
```

LOB: Plot the given points on the graph in order to verify if they lie on the same line or not

Of the given points A (0, 8), B (5, 5), C (10, 2) and D (8, 4), which one is not collinear?
 Option I: (0, 8)

Option 2: (5,5) Option 3: (10,2) Option 4: (8,4) Correct Answer: Option 4

2. If the points (4,0), (7,3) and (k,5) lies on the same line, what is the value of k?
Option 1: 5
Option 2: 8
Option 3: 9
Option 4: 10
Correct Answer: Option 3

LOB: Choose an appropriate scale in order to plot a graph for the given data

1. The table below shows the cost of parking for different hours.

| Hours | 2 | 4 | 6 | 8 | 10 |
|---------------|-----|-----|-----|-----|-----|
| Amount (in ì) | 160 | 320 | 480 | 640 | 800 |

Which of following options shows the appropriate scale to plot a graph of the given data? **Option I:** On horizontal axis, I unit = I hour; on vertical axis, I unit = I

Option 2: On horizontal axis, I unit = I hour; on vertical axis, I unit = 10 Option 3: On horizontal axis, I unit = I hour; on vertical axis, I unit = 160 Option 4: On horizontal axis, I unit = I hour; on vertical axis, I unit = 800 Correct Answer: Option 3

2. The table below shows the simple interest earned for different amount of sum deposited.

| Sum Deposited (in ì) | 1000 | 1500 | 2000 | 2500 | 3000 |
|------------------------|------|------|------|------|------|
| Interest Earned (in ì) | 80 | 120 | 160 | 200 | 240 |

Which of following graphs best represents the given data?





LOB: Construct the line graph in order to discuss the relationship between independent and dependent variable in a given mathematical situation

I. The table below shows the perimeter of a regular pentagon for different side lengths.

| Side length (in cm) | 3 | 5 | 7 | 8 |
|---------------------|----|----|----|----|
| Perimeter (in cm) | 15 | 25 | 35 | 40 |



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2. A swimming pool has a capacity of 375 cubic metres. A pump fills the empty pool at the constant rate shown in the graph.



Which of the following statements is correct the given data?
Option 1: The pump fills 25 cubic metres of water each minute.
Option 2: The pump fills 1 cubic metres of water in 25 minutes.
Option 3: The pump fills 50 cubic metres of water each minute.
Option 4: The pump will completely fill the tank in 25 minutes.
Correct Answer: Option 1

Suggested Teacher Resources



Lesson Plan



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| Objectives | Draw a line graph in order to represent the given data that changes continuously over periods of time | | |
|---------------------------|---|--|--|
| Objectives | Interpret the given line graph in order to answer the given questions | | |
| | Interpret the given line gruph in order to unover the given questions. | | |
| Prerequisite Knowledge | Basic knowledge of Cartesian plane. | | |
| | Chalk and blackboard. | | |
| Material | Pen/pencil and notebooks. | | |
| Required | Graph Papers. | | |
| Procedure | aw the following table on blackboard to represent the given data- | | |
| | The table below shows daily temperatures for New York City, recorded for 6 days, in degrees Fahrenheit. | | |
| | Temperatures In New York City | | |
| | Day Temperature | | |
| | I 43° F | | |
| | 2 53° F | | |
| | аранананананананананананананананананана | | |
| | 5 59° F | | |
| | 6 67° F | | |
| | low, draw the line graph of the given data with the help of the students using the following istructions- | | |
| | Step I: Draw and label the X-axis and the Y-axis on the board. Tell students that they will be learning about line graphs in this activity. Explain that a line graph uses points and lines to examine changes over time. Line graphs are often used when examining relationships between two types of information. | | |
| | Step 2: Tell students that, like the bar graph, the line graph has an X- and a Y-axis. The dependent variable is plotted on the Y-axis and usually measures quantity (percentage, Rupees, litres, etc.). The independent variable is plotted on the X-axis and usually measures time periods. Use the given data to complete your line graph on the board. Let's define the various parts of a line graph. | | |
| | | | |
| | title The title of the line graph tells us what the graph is about. | | |
| | labelsThe horizontal label across the bottom and the vertical label along the side tells us what kinds of facts are listed. | | |
| | scales The horizontal scale across the bottom and the vertical scale along the side tell us how much or how many. | | |





Objective: To collect, organise and represent the data graphically.

Step I: Ask a question to the class- how many first cousins do you have?

Step 2: Collect the responses. Suppose the responses are:

6,2,1,3,4,3,2,6,5,6,1,2,3,3,2,3,2,3,2,1,2,4,4,5,2,1,2,3,2,3,2,3,4,1,4,5,4,5,2,1,3,2,1,2,1.

Step 3: Ask the students- Do you find it difficult to identify which student has given which response? (Discuss) Step 4: Now, we will prepare a table in which the responses are mentioned in front of the student's name.

S.N Student Number of S.N Student Number of S.N Student Number of 0. Name cousins 0. Name cousins Name cousins 0. Shreya 1. Ramesh 16. Pooja 3 31. 6 2 17. 2. Shipra 2 Shantnu 2 32. Vani 3 3. Anuj 1 18. Ekansh 3 33. Amita 4 4. Ankit 3 19. Dimple 2 34. Pankai 1 Anit 4 20. Richa 5. 1 35. Anu 4 6. Mahima 3 21. Amit 2 36. Om 5 7. Priya 2 22. Vinit 4 37. 4 Jaya 8. Shikha 6 23. Sunil 4 38. Sushma 5 9. Reema 5 24. Dinesh 5 39. Sunita 2 10. 25. Yash Sonu 6 2 40 Neha 1 Monu Ashish 11. 26. 1 1 41. Atul 3 12. Shweta 2 27. Sohan 2 42. Akash 2 13. Silpa 3 28. Mohan 3 43. Alok 1 14. Renu 3 29. Rekha 2 44. Vinod 2 15. Ritu 2 30. Rajesh 3 45. Sharda

From this table we can clearly see the responses of each student. For instance, Ritu has only two cousins whereas Ramesh has six cousins.

Now ask the following questions from the students -

- I. What is the number of students who have the least number of cousins?
- 2. What is the number of students who have the highest number of cousins?
- 3. What is the number of students who have no cousins?
- 4. How many students have cousins more than 3 but less than 6?

The students would have to count for each of the above questions. To avoid any errors, the teacher and the students should make a frequency distribution table using tally marks for this data.

| No. of Cousins | Number of students | Frequency |
|----------------|--------------------|-----------|
| I | | 8 |
| 2 | ШШ | 14 |
| 3 | | 10 |
| 4 | Ш | 6 |
| 5 | | 4 |
| 6 | | 3 |
| | | 45 |

The students can now discuss the previous questions based on this table and also record other observations.

Step 5: To prepare a better visual representation, we can construct a bar graph for this data using the table.

The students will then construct a bar graph for this data which would look as below. The teacher will clear queries while the students attempt this.



Step 6: The teacher could now also ask the students to make a pie chart for this data.

Now again ask the same questions from the students.

This activity helps to understand the importance of graphs and give students the general understanding of how graphs are made out of the given data.

16. PLAYING WITH NUMBERS

QR Code:



Learning outcome and Learning Objectives:

| Content area / Concepts | Learning Objectives | Learning Outcome |
|----------------------------|--|----------------------------------|
| Numbers in | Use the concepts of place value in order to express | |
| General Form | the given numbers in their generalised form | |
| | Apply the divisibility rule of 11 in order to check | |
| | whether a given number is divisible by 11 or not | |
| | Add or subtract a two-digit number and its reverse in | |
| Comos with | order to check whether it is divisible by 9 or not | |
| Numbers | Subtract a three-digit number and its reverse in order | |
| inumbers | to verify that it is divisible by 99 | |
| | Form all possible three-digit numbers using the given | |
| | 3 digits in order to verify that the sum of these | |
| | numbers will be divisible by 37 | Observe patterns using algebraic |
| Lottors for Digits | Use addition and multiplication in order to find the | Observe patterns using algebraic |
| Letters for Digits | values of the letters in the given puzzles | divisibility rules of 2345698. |
| | Apply the divisibility rule of 10 in order to check | |
| | whether a given number is divisible by 10 or not | |
| | Apply the divisibility rule of 5 in order to check | |
| | whether a given number is divisible by 5 or not | |
| Tosts of | Apply the divisibility rule of 2 in order to check | |
| Divisibility | whether a given number is divisible by 2 or not | |
| | Apply the divisibility rule of 3 and 9 in order to check | |
| | whether a given number is divisible by them | |
| | Apply the divisibility rule of 2,5 and 10 in order to | |
| | check whether a given number is divisible by all of | |
| | them or not. | |

Test items



LOB: Use the concepts of place value in order to express the given numbers in their generalised form $(22 = 2 \times 10 + 2 \times 1)$

I. Which out of these is a generalized form of 405?

Option 1: $4 \times 10 + 5 \times 1$ Option 2: $4 \times 100 + 0 \times 10 + 5 \times 1$ Option 3: $4 \times 1000 + 0 \times 100 + 5 \times 10$ Option 4: $4 \times 100 + 5 \times 10$ Correct Answer: Option 2

- 2. Which of the following statements are correct?
 - a) The generalized form of a number xyz is 100x + 10y + z
 - b) The generalized form of a number and its reverse is the same.

Option I: Only a) is correct Option 2: Only b) is correct Option 3: Both a) and b) are correct Option 4: Neither a) nor b) is correct Correct Answer: Option I

LOB: Apply the divisibility rule of 11 in order to check whether a given number is divisible by 11 or not

I. Which of the following numbers is divisible by 11?

Option 1: 710098 Option 2: 741889 Option 3: 759066 Option 4: 771124 Correct Answer: Option 3

What value of k would make the number 75k077 divisible by 11?
Option 1: 0
Option 2: 6
Option 3: 8
Option 4: 9
Correct Answer: Option 4

LOB: Add or subtract a two-digit number and its reverse in order to check whether it is divisible by 9 or not.

I. Which of the following options make the statement below true?

If a > b, then ab - ba is divisible by _____ as ab - ba can be written as _____ Option 1: 9; 9(a - b)Option 2: 9; 9(a + b)Option 3: 6; 9(a - b)Option 4: 6; 9(a + b)Correct Answer: Option 1

- 2. Which of the following numbers obtained as a result of these operations are divisible by 9?
 - a) 76–67
 - b) 98-89
 - c) 21-12

Option I: c and a Option 2: b and c Option 3: a and b

Option 4: a, b, and c **Correct Answer:** Option 4

LOB: Subtract a three-digit number and its reverse in order to verify that it is divisible by 99.

I. Which of the following options make the statement below true?

If a > c, then abc - cba is divisible by ______ abc - cba can be written as _____ Option 1: 99; 99(a - c)Option 2: 99; 99(a + c)Option 3: 100; 100(a - c)Option 4: 100; 100(a + c)Correct Answer: Option 1

2. By which number would the numbers obtained as a result of the following operations are divisible?

```
a) 756–657
```

```
b) 908-809
```

```
c) 921-129
```

```
Option 1: 99
Option 2: 22
Option 3: 66
Option 4: 33
Correct Answer: Option 1
```

LOB: Form all possible three-digit numbers using the given 3 digits in order to verify that the sum of these numbers will be divisible by 37

I. By what number is the sum of 678+867+786?

Option 1: 36 Option 2: 37 Option 3: 46 Option 4: 47 Correct Answer: Option 2

Consider the number abc, where a,b and c numbers from 1 to 9 and . Which of these is divisible by 111?
 Option 1: abc + bca + cab
 Option 2: abc + bac + cab
 Option 3: acb + bca + cab
 Option 4: acb + bac + cab
 Correct Answer: Option 1

LOB: Use addition and multiplication in order to find the values of the letters in the given puzzles

I. Which of the following options make the puzzle below true?

Option 1: Z=9, Y=6 Option 2: Z=4, Y=9 Option 3: Z=4, Y=6 Option 4: Z=6, Y=6 Correct Answer: Option 3

2. What values of A and B will make the puzzle below true?

ABA × 5 44B0 **Option I**: A=9, B=8 **Option 2:** A=8, B=9 **Option 3**: A=4, B=2 **Option 4**: A=4, B=2 **Correct Answer:** Option 2 LOB: Apply the divisibility rule of 10 in order to check whether a given number is divisible by 10 or not I. Which of the following numbers is divisible by 10? **Option 1:** 3390 **Option 2:** 3445 **Option 3**: 4039 **Option 4**: 7601 Correct Answer: Option 1 2. What value of X and Y would make the number 90Y77X divisible by 10? **Option I**: X=0 and Y can be any number from 1 to 9 Option 2: Y=0 and X can be any number from 1 to 9 **Option 3**: X=5 and Y =0 **Option 4**: X=7 and Y =5 Correct Answer: Option I LOB: Apply the divisibility rule of 5 in order to check whether a given number is divisible by 5 or not I. Which of the following numbers is divisible by 5? **Option I**: 1355 **Option 2:** 2411 **Option 3**: 3198 **Option 4**: 4466 Correct Answer: Option 1 2. What value of X and Y would make the number Y77X divisible by 5? **Option I:** Y=0 and X can be any number from 1 to 9 **Option 2**: X=6 and Y =9 **Option 3**: X=7 and Y =5 Option 4: X=0 or 5 and Y can be any number from 1 to 9 **Correct Answer:** Option 4 LOB: Apply the divisibility rule of 2 in order to check whether a given number is divisible by 2 or not I. Which of the following options show a list of numbers which are divisible by 2? **Option I**: 67; 896789; 9087 **Option 2:** 67543; 98; 98456 **Option 3**: 98456; 870956; 854780 **Option 4**: 67453; 898; 9076 Correct Answer: Option 3 **2.** What value of X and Z would make the number 98ZX divisible by 2? **Option I:** Z=0 and X can be any number from I to 9 **Option 2**: X=9 and Z =9 **Option 3**: X=4 and Z =5 Option 4: X=7 and Z=6

Correct Answer: Option 3

LOB: Apply the divisibility rule of 3 and 9 in order to check whether a given number is divisible by them.

- Which of the following options show a list of numbers which are all divisible by 3?
 Option 1: 672; 96789; 9087
 Option 2: 60043; 98; 98456
 Option 3: 98456; 870956; 854780
 Option 4: 67453; 898; 9076
 Correct Answer: Option 1
- What value of digits A and B would make the number 894A5B divisible by 3?
 Option 1: A=3 and B=1
 Option 2: A=2 and B=1
 Option 3: A=3 and B=4
 Option 4: A=4 and B=2
 Correct Answer: Option 1

LOB: Apply the divisibility rule of 2,5 and 10 in order to check whether a given number is divisible by all of them or not.

 Which of the following options make the statement below true? A number divisible by 10 would always has its one's digit as _ and a number divisible by 5 always has the one's digit as __.

Option 1: 0; 0 or 5 Option 2: 0; 5 Option 3: 0 and 5; 0 and 5 Option 4: 0; 0 Correct Answer: Option 1

- 2. By what number would a sum of two even numbers be always divisible?
 - Option 1: 2 Option 2: 4 Option 3: 5 Option 4: 6 Correct Answer: Option 1

Suggested Teacher Resources



Lesson Plan



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| Objectives | Apply the divisibility rule of 3 and 9 in order to check whether a given number is divisible by them | | | | |
|---------------------------|---|--|--|--|--|
| Prerequisite Knowledge | Simple Division, divisibility rules of 2, 4, 5, 8 and 10. | | | | |
| Material Required | Chalk and blackboard. Pen/Pencil and notebook | | | | |
| Procedure | Start the class with the following activity- | | | | |
| | Write down a few numbers on the board as below: | | | | |
| | 5, 10, 24, 25, 115, 975, 4646, 625, 216, 920, 5280, 44420 | | | | |
| | | | | | |
| | | | | | |
| | | | | | |
| | Create a table separately mentioning numbers 2, 4, 5, 8 and 10 as column headers. Ask the students to place each number from the list under the column(s) that is a factor of the number. For example, if 32 was in the list, it would be placed under 2, 4 and 8, because they are all its factors.Give 5 minutes to the students to attempt this task.After 5 minutes, the teacher can ask the students to raise hands to fill the table on the board and also give reasons while doing so. The table would now look as below:5, 10, 24, 25, 115, 975, 4646, 625, 216, 920, 5280, 44420 | | | | |
| | 216, 920, 5280, 5280, 44420 975, 625, 920, 5280, 44420 44420 5280, 44420 5280, 44420 | | | | |
| | Note: During this task, most students would have used the divisibility rules of 2, 4, 5, 8 and 10 to do this. Discuss them in case students have any doubt. The teachers can also take different numbers in their class. Now, move on to discuss the divisibility rules of 3 and 9. Write a few numbers which students already know have 3 or 9 as their factors. What do the numbers 12, 15, 18, 27, 30, 66, and 93, 102 all have in common? Each is divisible by 3. Calculate the sum of the digits for each given number. For example, the sum of the digits in the number 12 is 3 because 1 + 2 = 3. | | | | |

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| Give students time to find the sums. Record the sums on the board. | | |
|--|--------|-------------------|
| | Number | Sum of its digits |
| | 12 | I+2=3 |
| | 15 | I+5=6 |
| | 18 | I+8=9 |
| | 27 | 2+7=9 |
| | 30 | 3+0=3 |
| | 66 | 6+6=12 |
| | 93 | 9+3=12 |
| | 114 | + +4=6 |

Now based on the table ask the following questions:

What do these sums in column 2 have in common?

They are divisible by 3.

When the sum of a number's digits is divisible by 3, the entire number is divisible by 3. This is the divisibility rule for 3.

Now let's examine a different set of numbers: 27, 36, 45, 54, 63 72, 90, 108. What do these numbers have in common?

They are divisible by 9.

Now ask the students to calculate the sum of the digits for each given number as done earlier. Record the sums on the board.

| Number | Sum of its digits |
|--------|-------------------|
| 27 | 2+7=9 |
| 36 | 3+6=9 |
| 45 | 4+5=9 |
| 54 | 5+4=9 |
| 63 | 6+3=9 |
| 72 | 7+2=9 |
| 108 | 1+0+8=9 |
| 44 | +4+4=9 |

We can observe that all the sums in column 2 are divisible by 9.

When the sum of a number's digits is divisible by 3 and 9, the entire number is divisible by 9. This is the divisibility rule for 9.

Now let us consider a big number like 1503. This number is divisible by both 3 and 9. We can represent 1503 in the expanded form as

 $1 \times 1000 + 5 \times 100 + 0 \times 10 + 3 \times 1$

Let's decompose 1000 to 999+1 and 100 to 99+1 (999 and 99 are divisible by 3 and 9). $1 \times 1000 + 5 \times 100 + 0 \times 10 + 3 \times 1 = 1(999 + 1) + 5(99 + 1) + 3 \times 1$ Now use the distributive property,

 $1(999 + 1) + 5(99 + 1) + 3 \times 1 = 1 \times 999 + 1 \times 1 + 5 \times 99 + 5 \times 1 + 3 \times 1$ Since we know that 9 is divisible by both 3 and 9, we will now factor the 9 out of the expression. We can use the commutative and associative properties for this.

 $\begin{array}{c} 999+5\times99+5+3+1\\ 111(9)+5\times11(9)+5+3+1\\ 9\times111+9\times5\times11+5+3+1\\ 9(111+5\times11)+5+3+1 \end{array}$

| | We know that the product of $9(111 + 5 \times 11)$ is divisible by 9 since 9 is already factored out. Since the first term is divisible by 3 and 9, the number 1503 is divisible by 3 and 9 if and only if $5 + 3 + 1$ is also divisible by 3 and 9. |
|-----------|--|
| | The sum of $5 + 3 + 1$ is 9. That means it is also divisible by 3 and 9 as both 3 and 9 are factors of 9. |
| | 5 + 3 + 1, these three digits are part of our original number. |
| | Also, explain to the students that if a number is divisible by 9, it is divisible by 3 as well as $9=3 \times 3$. But if any number is divisible by 3, it is not necessarily divisible by 9. For example, 12, 24, 42 are divisible by 3 but are not divisible by 9. |
| Reference | https://www.engageny.org/sites/default/files/downloadable-resources/math-g6-m2-topic-d- lesson-17-teacher.pdf |



The following puzzle can be given to the students to solve.

The digits are distinct whole numbers. Solve for A, B and C, given that:



Students should be given some time to explore and try to solve it on their own.

There could be different ways to solve this. Two of them have been discussed below:

Method I:

We have been given three two-digit numbers which are being added and their sum is a three-digit number. Any two-digit number XY could be expressed as 10X+Y and any three digit number XYZ could be expressed as 100X + 10Y + Z. So, we can write,

We have been given that

| AA + BB + | CC = ABC |
|----------------|----------------|
| AA + BB + CC = | 100A + 10B + C |

We can write it as

$$11A + 11B + 11C = 100A + 10B + C$$

We can take 11 common in the left-hand side of the equation, which could be shown as below: 11(A + B + C) = 100A + 10B + C

This means that the number ABC is divisible by 11. By the divisibility rule of 11, we know that any whole number is divisible by 11 if the sum of the digits at even position = sum of the digits at the odd position.
A + C = B

So,

Substituting this in above,

11(A + B + C) = 100A + 10B + C 11(A + A + C + C) = 100A + 10(A + C) + C $11 \times 2(A + C) = 100A + 10A + 10C + C$ 22(A + C) = 110A + 11C 22A + 22C = 110A + 11C 11C = 88AC = 8A

Since A, B and C are distinct whole numbers, the only possible value for A here is 1. A = 1, C = 8(1) = 8

$$B = A + C = 1 + 8 = 9$$

Therefore, the number ABC is 189.

Method 2:

| AA |
|------|
| BB |
| + CC |
| ABC |

We have been given that three two-digit numbers are added and the sum is a three-digit number.

The largest possible value for ABC could be 99 + 88 + 77 = 264.

(Even if we were not given the condition that A, B and C are distinct, then also the largest possible value for ABC would be less than 300. Think about this!)

Considering the largest possible value of ABC is 264, there are only two choices left for A, i.e., A=1 or A=2.

Also, if we look at the ones place of the resultant, we can see that

A + B + C = C

Which implies that A + B = 10, so that a carryover can be taken and C remains in the ones place of ABC. The two possible cases are:

| Case(i) | Case(ii) |
|---|--|
| If $A = 1$, then $B = 9$. | If $A = 2$, then $B = 8$. |
| So, $AA + BB + CC = ABC$ | So, $AA + BB + CC = ABC$ |
| 11 + 99 + CC = 19C | 22 + 88 + CC = 28C |
| 110 + CC = 19C | 110 + CC = 28C |
| Now, if we focus on the one's column, we have | Now, if we focus on the one's column, we have |
| 0+C=C | 0+C=C |
| If we focus on the ten's column, we have | If we focus on the ten's column, we have |
| 1 + C = 9 | 1 + C = 8 |
| <i>i.e.</i> , <i>C</i> = 8 | i. e., C = 7 |
| | If $C = 7$, then |
| 110 + 88 = 198 | AA + BB + CC = 110 + 77 = 187 |
| | Which is not possible as we have considered A=2? |
| This way, we get the number ABC as 198. | Hence this solution is incorrect. |

This way, we get the number ABC as 198.

Reference: https://mindyourdecisions.com/2016/05/22/aa-bb-cc-abc-sunday-puzzle/